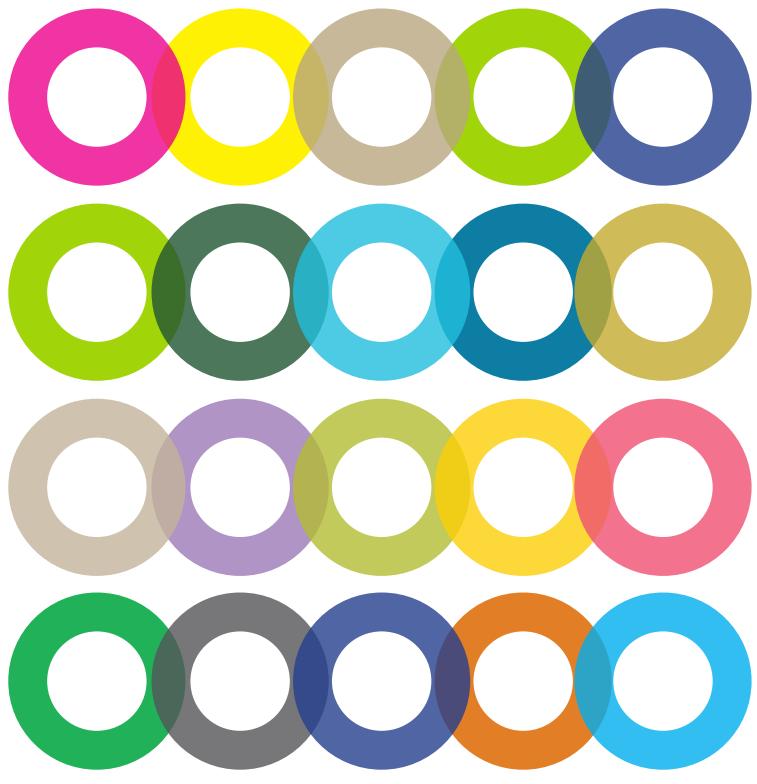
MATHEMATICS UTAH CORE GUIDES GRADE 4



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Core Guide

Use the four operations with whole numbers (addition, subtraction, multiplication, and division) to solve problems (Standards 4.OA.1–3).

Standard 4.OA.1 Interpret a multiplication equation as a comparison (for example, interpret 35 = 5 × 7 as a statement that 35 is 5 times as many as 7 and 7 times as many as 5). Represent verbal statements of multiplicative comparisons as multiplication equations.

Concepts and Skills to Master

- Distinguish between additive comparisons and multiplicative comparisons (8 can be compared to 2 additively, 8 is 6 more than 2 and can also be compared to 2 multiplicatively, 8 is 4 times as many as 2)
- Recognize that any two factors and their product can be read as a comparison (8 is 4 times as many as 2, or 2 times as many as 4 is 8)
- Write multiplication equations from multiplicative comparison situations
- Represent multiplicative comparisons using a variety of models and strategies

Teacher Note: Fourth grade is the first time that students view multiplication as a comparison. In first and second grade, students work with additive comparisons. Third grade students understand multiplication as groups or arrays of objects. In fourth grade, these understanding extend to multiplication as a comparison. Multiplicative comparison situations are more complex than equal groups and arrays, and must be carefully distinguished from additive comparison problems. This standard should be taught with Standard 4.OA.2 using the following multiplication and division situations. (See: TABLE 2. Common multiplication and division situations.)

- Compare/Larger Unknown word problems (A blue hat costs \$3. A red hat costs 4 times as much as the blue hat. How much does the red hat cost?)
- **Compare/Smaller Unknown** word problems (A red hat costs \$12 and that is 4 times as much as a blue hat costs. How much does a blue hat cost?)
- Compare/Multiplier Unknown word problems (A red hat costs \$12 and a blue hat costs \$3. How many times as much does the red hat cost as the blue hat?)

Related Standards: Current Grade Level	Related Standards: Future Grade Levels		
 4.OA.2 Multiply and divide to solve word problems involving multiplicative comparisons 4.OA.3 Solve multi-step word problems using whole numbers and having whole-number answers using the four operations 4.MD.1 Within a single system of measurement, express measurements in a larger unit in terms of a smaller unit 4.NF.4 Apply and extend understanding of multiplication to multiply a fraction by a whole number 	 5.NF.3 Interpret a fraction as division of the numerator by the denominator 5.NF.4, 5.NF.5 Apply and extend previous understandings of multiplication and division to multiply a fraction or whole number by a fraction 6.RP.1 Understand the concept of a ratio 		
Critical Background Knowledge from Previous Grade Levels			
 Interpret products of whole numbers and whole-number quotients (3.OA.1, 3.OA.2) Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities (3.OA.3) Use addition and subtraction to two-step solve word problems comparing unknowns in all positions (2.OA.1) 			
Academic Vocabulary			
multiply, compare, multiplicative comparison, additive comparison, equation, array, factor, product			

perations and Algebraic Thinking				Grade 4
uggested Models			Suggested Strategies	
Unknown Product	Group Size Unknown How many in each group?	Number of Groups Unknown How many groups?	 Use bar models, number lines, equations, and context to represer multiplicative comparison Use concrete models such as connecting cubes, Cuisinare Rods, et 	
Multiplicative Comparison B \$6 R	\$18 R B ?	\$18 R \$6 B \$6		
? 3 × 6 = ?	$3 \times ? = 18$ $18 \div 3 = ?$	$? \times 6 = 18$ $18 \div 6 = ?$		
General $a \times b = ?$	$a \times ? = p$, and $p \div a = ?$	$? \times b = p$, and $p \div b = ?$		

Core Guide

Use the four operations (addition, subtraction, multiplication, and division) with whole numbers to solve problems (Standards 4.OA.1–3).

Standard 4.OA.2 Multiply or divide to solve word problems involving multiplicative comparison, for example, by using drawings and equations with a symbol for the unknown number to represent the problem, distinguishing multiplicative comparison from additive comparison.

Concepts and Skills to Master

- Solve the following types of comparison multiplication and division situations
- Compare/Larger Unknown word problems (A blue hat costs \$3. A red hat costs 4 times as much as the blue hat. How much does the red hat cost?)
- Compare/Smaller Unknown word problems (A red hat costs \$12 and that is 4 times as much as a blue hat costs. How much does a blue hat cost?)
- Compare/Multiplier Unknown word problems (A red hat costs \$12 & a blue hat costs \$3. How many times as much does the red hat cost as the blue hat?)

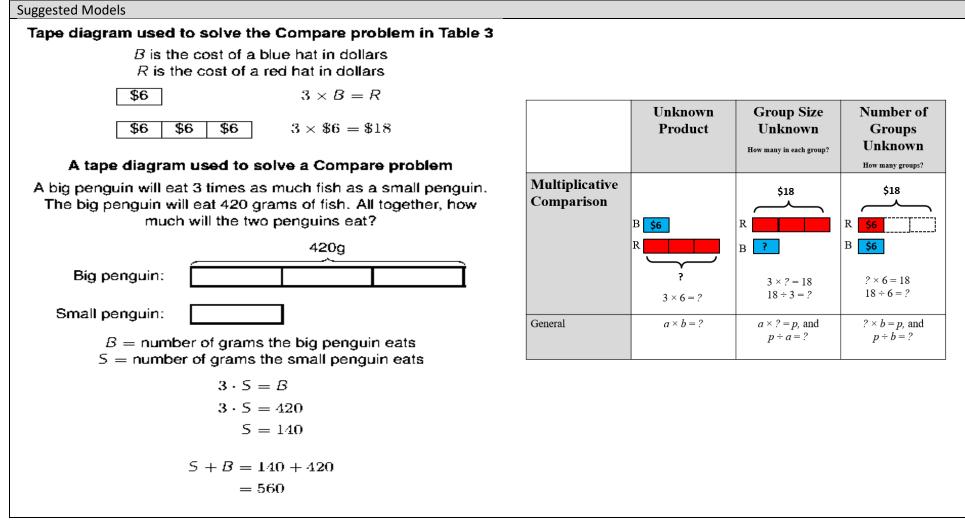
Teacher Note: Fourth grade is the first time that students view multiplication as a comparison. In first and second grade, students work with additive comparisons. Third grade students understand multiplication as groups or arrays of objects. In fourth grade, these understanding extend to multiplication as a comparison. Multiplicative comparison situations are more complex than equal groups and arrays, and must be carefully distinguished from additive comparison problems. This standard should be taught with standard 4.OA.1.

Related Standards: Current Grade Level	Related Standards: Future Grade Levels
4.OA.3 Solve multi-step word problems using whole numbers and	5.NF.3 Interpret a fraction as division of the numerator by the denominator
having whole-number answers using the four operations	5.NF.4 Apply and extend previous understandings of multiplication and division to
4.OA.1 Interpret multiplication as comparison	multiply a fraction or a whole number by a fraction
4.MD.1 Within a single system of measurement, express	5.NF.5 Interpret multiplication as scaling
measurements in a larger unit in terms of a smaller unit	5.OA.2 Write and interpret numerical expressions
4.NF.4 Apply and extend understanding of multiplication to	5.NF.6 Extend previous understanding of multiplication and division to multiply and
multiply a fraction by a whole number	divide fractions
4.NF.1 Extend understanding of fraction equivalence and ordering	6.RP.1 , 6.RP.2. Understand the concept of a ratio and solve ratio problems
Critical Background Knowledge from Previous Grade Levels	
• Interpret products of whole numbers and whole-number quotient	is (3.0A.1, 3.0A.2)
• Use addition and subtraction to word problems comparing with ur	nknowns in all positions (2.OA.1)
Academic Vocabulary	
multiplicative comparison, additive comparison	
Suggested Strategies	

Suggested Strategies

• Use bar models, number lines, equations, and context to represent multiplicative comparison

• Use concrete models such as connecting cubes, Cuisinare Rods, etc.



Operations and Algebraic Thinking Core Guide Grade 4 Use the four operations with whole numbers (addition, subtraction, multiplication, and division) to solve problems (Standards 4.0A.1–3). Standard 4.OA.3 Solve multi-step word problems posed with whole numbers and having whole-number answers using the four operations, including problems in which remainders must be interpreted. **a.** Represent these problems using equations with a letter standing for the unknown quantity. **b.** Assess the reasonableness of answers using mental computation and estimation strategies, including rounding. Concepts and Skills to Master • Differentiate between one-step and two-step word problems (Two-step word problems may include any combination of two operations in the same problem) Determine the operation(s) based on the actions in the context of multi-step word problems (avoid relying on keyword strategies) • Use numbers and symbols to represent word problems $(+, -, \times, \div, =, \text{ and a letter for unknowns})$ • Know that multiplication and division are performed (in the order they appear in the problem; from left to right) prior to addition and subtraction (in the order they appear in the problem; from left to right) Interpret remainders when necessary. Determine the reasonableness of the calculated answer using mental computation and estimation strategies **Related Standards: Current Grade Levels Related Standards: Future Grade Levels** 4.OA.2 Multiply and divide to solve word problems involving multiplicative comparisons 5.NF.2 Solve real-world problems involving addition and subtraction of fractions referring to the same whole, including **4.OA.3** Solve multi-step word problems using whole numbers and having whole-number answers using the four operations cases of unlike denominators. Use benchmark fractions and **4.NBT.3** Use place value understanding to round multi-digit whole numbers to any place number sense of fractions to estimate mentally and assess the 4.NBT.4 Fluently add and subtract multi-digit whole numbers using the standard algorithm reasonableness of answers **4.NBT.5** Multiply a whole number of up to four digits by a one-digit whole number, and 5.NF.6 Solve real-world problems involving multiplication of multiply two two-digit numbers fractions and mixed numbers 4.NBT.6 Find whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division Critical Background Knowledge from Previous Grade Levels Interpret products of whole numbers and whole-number quotients (3.OA.1, 3.OA.2) • Determine the unknown whole number in a multiplication or division equations (3.OA.4) • Apply properties of operations as strategies to multiply and divide (3.OA.5) • Understand the relationship between multiplication and division (3.OA.6) • Fluently multiply and divide (3.OA.7) Represent & solve two-step problems using equations with a letter standing for the unknown (3.OA.8) • Use addition and subtraction within 100 to solve one-step and two-step problems (2.OA.2) Academic Vocabulary multi-step word problem, mental math, estimation, rounding, remainder, variable, operations, equation, reasonableness, inverse operations, multiplicative comparison, additive comparison, symbol

Operations and Algebraic Thinking	Core Guide	Grade 4
Suggested Models	Suggested Strategies	
A two-step problem with diagram showing problem situation and equations showing the two parts Carla has 4 packages of silly bands. Each package has 8 silly bands in it. Agustin is supposed to get 15 fewer silly bands than Carla. How many silly bands should Agustin get? Carla:	 Use drawings, objects, and equations Use a bar model Apply Part/Part/Whole Create student-generated word problems Skip count Use the relationship between multiplication and division 	
Image Source: https://commoncoretools.files.wordpress.com/2011,	/05/ccss_progression_cc_oa_k5_2011_05_302.pdf	

TABLE 2. Common	multiplication	and division	situations. ¹
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	Unknown Product 3 × 6 = ?	Group Size Unknown ("How many in each group?" Division) 3 × ? = 18 and 18 ÷ 3 = ?	Number of Groups Unknown ("How many groups?" Division) ? × 6 = 18 and 18 ÷ 6 = ?
EQUAL GROUPS	There are 3 bags with 6 plums in each bag. How many plums are there in all? <i>Measurement example.</i> You need 3 lengths of string, each 6 inches long. How much string will you need altogether?	If 18 plums are shared equally into 3 bags, then how many plums will be in each bag? <i>Measurement example.</i> You have 18 inches of string, which you will cut into 3 equal pieces. How long will each piece of string be?	If 18 plums are to be packed 6 to a bag, then how many bags are needed? <i>Measurement example.</i> You have 18 inches of string, which you will cut into pieces that are 6 inches long. How many pieces of string will you have?
ARRAYS ²	There are 3 rows of apples with 6 apples in each row. How many apples are there?	If 18 apples are arranged into 3 equal rows, how many apples will be in each row?	If 18 apples are arranged into equal rows of 6 apples, how many rows will there be?
AREA ³	What is the area of a 3 cm by 6 cm rectangle?	A rectangle has area 18 square centimeters. If one side is 3 cm long, how long is a side next to it?	A rectangle has area 18 square centimeters. If one side is 6 cm long, how long is a side next to it?
COMPARE ⁴	A blue hat costs \$6. A red hat costs 3 times as much as the blue hat. How much does the red hat cost? Measurement example. A rubber band is 6 cm long. How long will the rubber band be when it is stretched to be 3 times as long?	A red hat costs \$18 and that is 3 times as much as a blue hat costs. How much does a blue hat cost? Measurement example. A rubber band is stretched to be 18 cm long and that is 3 times as long as it was at first. How long was the rub- ber band at first?	A red hat costs \$18 and a blue hat costs \$6. How many times as much does the red hat cost as the blue hat? Measurement example. A rubber band was 6 cm long at first. Now it is stretched to be 18 cm long. How many times as long is the rubber band now as it was at first?
GENERAL	a × b = ?	$a \times ? = p$ and $p \div a = ?$	$? \times b = p \text{ and } p \div b = ?$

¹ The first examples in each cell are examples of discrete things. These are easier for students and should be given before the measurement examples.

- ² The language in the array examples shows the easiest form of array problems. A harder form is to use the terms rows and columns: The apples in the grocery window are in 3 rows and 6 columns. How many apples are in there? Both forms are valuable.
- ³ Area involves arrays of squares that have been pushed together so that there are no gaps or overlaps, so array problems include these especially important measurement situations.
- ⁴ Multiplicative Compare problems appear first in Grade 4, with whole-number values in all places, and with the "times as much" language in the table. In Grade 5, unit fractions language such as "one third as much" may be used. Multiplying and unit fraction language change the subject of the comparing sentence, e.g., "A red hat costs A times as much as the blue hat" results in the same comparison as "A blue hat costs 1/A times as much as the red hat," but has a different subject.

Operations and Algebraic Thinking

Core Guide

Gain familiarity with factors and multiples (Standard 4.OA.4).				
Standard 4.OA.4 Find all factor pairs for a whole number in the range 1-100. Recognize that a whole number is a multiple of each of its factors. Determine				
whether a given whole number in the range 1-100 is a multiple of a given one-	whether a given whole number in the range 1-100 is a multiple of a given one-digit number. Determine whether a given whole number in the range 1-100 is			
prime or composite.				
Concepts and Skills to Master				
 Understand factor pairs as two whole numbers that multiply together to g 	get one product			
 Understand that prime numbers have exactly one factor pair 				
 Understand that composite numbers have more than one factor pair 				
 Understand multiples as a product of two given whole numbers. 				
 List the multiples of the numbers 2 through 9 up to 100 				
Create a list or chart of factor pairs of whole numbers 1-100				
Identify, from a list or chart, which whole numbers are prime or composit				
Teacher Note: The number 1 is neither prime nor composite. A prime number	er is a number greater than 1 that has o	niy 2 factors, 1 and itself. Composite		
numbers have more than 2 factors.	Deleted Standarder Friture Crede Lave	la la		
Related Standards: Current Grade Level 4.NBT.5 Multiply a whole number of up to four digits by a one-digit whole	Related Standards: Future Grade Leve			
number and multiply two two-digit numbers	whole numbers	tor and least common multiple of two		
4.NBT.6 Find whole-number quotients with up to four-digit divisors and	whole humbers			
one-digit dividends				
Critical Background Knowledge from Previous Grade Levels				
Determine unknown whole numbers in multiplication and division equation	ons (3 0A 4)			
 Understand the relationship between multiplication and division (3.OA.6) 				
 Fluently multiply and divide (3.0A.7) 				
 Identify and explain arithmetic patterns in multiplication and addition tab 	les (3.OA.9)			
Academic Vocabulary				
factor, factor pairs, multiple, prime, composite, whole number				
Suggested Models		Suggest Strategies		
		Use counters to build rectangular		
The number 12 can be made into several different rectangular arrays The nu	Imber 7 can only be made into one	arrays		
	gular array and is therefore a prime	 Use tools such as number lines, 		
numbe		hundreds charts, arrays, or cubes to		
		model relationships between		
		factors and multiples		

Generate and analyze numeric and shape patterns (Standard 4.OA.5). Standard 4.OA.5 Generate a number or shape pattern that follows a given rule. Identify apparent features of the pattern that were not explicit in the rule itself. For example, given the rule "add 3" and the starting number 1, generate terms in the resulting sequence and observe that the terms appear to alternate between odd and even numbers. Explain informally why the numbers will continue to alternate in this way. Concepts and Skills to Master • Understand that number and shape patterns follow a given rule • Understand that there are sometimes features of the pattern that are not stated in the rule • Complete a given number or shape pattern (e.g., 3, 6, 9, ____, 18) • Determine the rule of a given pattern (e.g., 3, 6, 9, 12, 15, 18, ... The rule is to skip count by 3 or multiples of 3) • Generate a number or shape pattern that follows a rule and state the rule Identify and state any alternate features of the pattern that are not stated in the rule • Extend a given number or shape pattern using manipulatives, skip counting, pictures, etc. Teacher Note: Although students find the given rule to a pattern, they are not required to use variables to explain or write the related expression. Emphasis should be placed on patterns with one-step; although, students may be exposed to patterns with two-steps. Related Standards: Current Grade Level Related Standards: Future Grade Levels 4.OA.3 Solve multi-step word problems and 5.OA.3 Generate two numerical patterns using two given rules, identify relationships between represent these problems with equations that use corresponding terms, and form ordered pairs for graphing on a coordinate plane 6.EE.2 Write, read, and evaluate expressions in which letters represent numbers variables **6.EE.9** Use variables to represent two quantities that change in relationship to one another and write expressions to express one quantity in terms of the other quantity **6.RP.1** Understand the concept of a ratio and use ratio language to describe a relationship between two quantities Critical Background Knowledge from Previous Grade Levels Identify and explain arithmetic patterns (3.OA.9) • Determine whether a group of objects (up to 20) has an odd or even number of members (2.OA.3) Academic Vocabulary number pattern, shape pattern, pattern rule, sequence, input/output table

Core Guide

4.0A.5

Operations and Algebraic Thinking

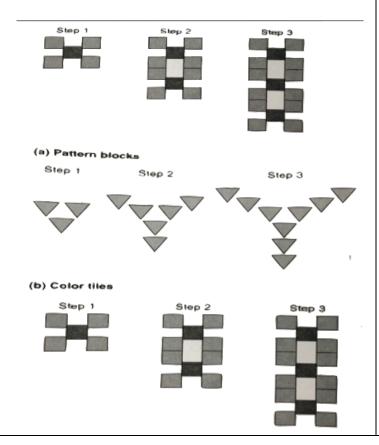
Grade 4

Suggested Models

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

What is the rule of the pattern? *Start at 4 and add 3*

What do you notice about this pattern? even, odd, even, odd, even, odd, ... It looks like stairs with two white steps in between Write a context or story to match this pattern. It costs \$4 to play a game and \$3 for each additional game



Suggested Strategies

- Create and describe patterns in number charts
- Create and describe patterns using pattern blocks, colored tiles, cubes paper squares, etc.
- Create and work with tables
- Use input-output tables
- Write sequences forwards and backwards
- Predict terms that come later in given patterns

Number and Operations in Base Ten

Core Guide

Generalize place value understanding for multi-digit whole numbers by analyzing patterns, writing whole numbers in a variety of ways, making comparisons, and rounding (Standards 4.NBT.1–3)

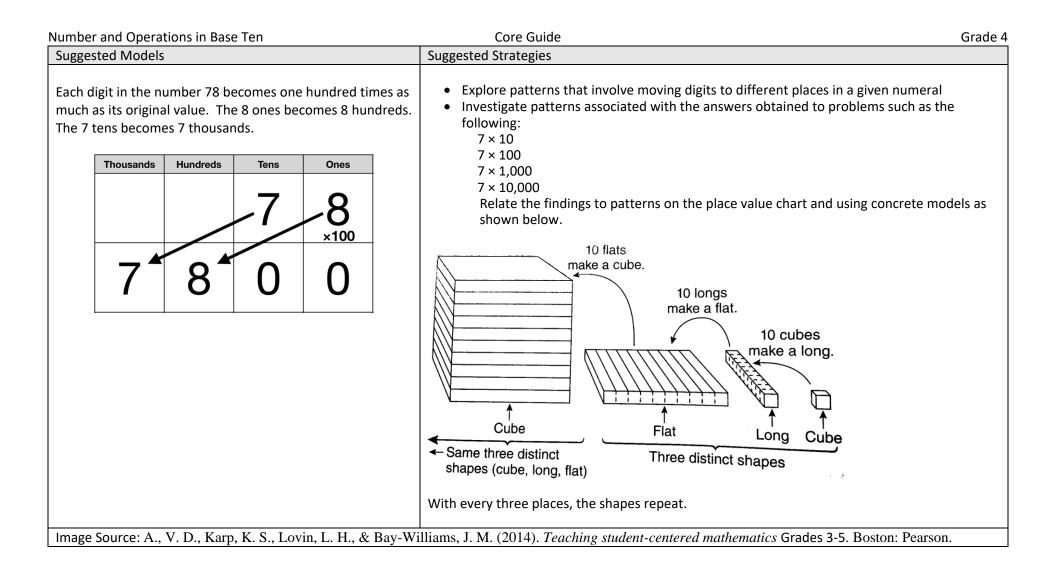
Standard 4.NBT.1 Recognize that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right. For example, recognize that 700 ÷ 70 = 10 by applying concepts of place value and division.

Concepts and Skills to Master

- Understand the places of numbers and the value of each place
- Model place and value relationships showing how a digit in one place represents ten times what it represents in the place to its right (Use manipulatives such as place value blocks, mats, discs, etc.)
- Understand that the value of each place is ten times greater than the place to the right
- Understand that the value of each place is ten times less than the place to the left
- Multiply and divide numbers by multiples of tens, hundreds, thousands, etc. to one million (For example: $70 \times 100 = 7,000$ 5,000 $\times 10 = 50,000$ and $700 \div 70 = 10$ 50,000 $\div 50 = 1,000$)

Teacher Note: This standard is a prerequisite to 5.NBT.1 and 5.NBT.2, where students will describe the shifting of digits when multiplying and dividing numbers by multiples of ten.

Related Standards: Current Grade Level	Related Standards: Future Grade Levels		
 4.OA.1–2 Interpret a multiplication equation as a comparison 4.NBT.2 Read and write multi-digit whole numbers using base-ten numerals, number names, and expanded form 4.NBT.3 Use place value understanding to round multi-digit whole numbers to any place 4.NBT.4 Fluently add and subtract multi-digit whole numbers 4.NBT.5 Multiply a whole number up to four digits by a one-digit whole number, and multiply two two-digit numbers using strategies based on place value 4.NBT.6 Find whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, using strategies based on place value 	 5.NBT.1 Recognize that in a multi-digit number, a digit in one place represent 10 times as much as it represents in the place to its right and 1/10 of what it represents in the place to its left. 5.NBT.2 Explain patterns in the numbers of zeros of the product when multiplying a number by powers of 10 		
Critical Background Knowledge from Previous Grade Levels			
 Multiply one-digit whole numbers by multiples of ten (3.NBT.3) Represent and solve problems involving multiplication and division within 100 (3.OA.1–4, 7) Understand the relationship between multiplication and division and fluently multiply and divide within 100 (3.OA.5–6) Understand that the three digits of a three-digit number represent amounts of hundreds, tens, and ones (2.NBT.1) 			
Academic Vocabulary			
inverse operation, base ten numeral (standard form), value, place, and place value, digit, m	nultiply, divide		



Number and Operations in Base Ten

Core Guide

Generalize place value understanding for multi-digit whole numbers by analyzing patterns, writing whole numbers in a variety of ways, making comparisons, and rounding (Standards 4.NBT.1–3)

Standard 4.NBT.2 Read and write multi-digit whole numbers using base-ten numerals, number names, and expanded form. Compare two multi-digit numbers based on meanings of the digits in each place, using >, =, and < symbols to record the results of comparisons.

Concepts and Skills to Master

- Express a given number in multiple ways:
 - base-ten numerals (42,371)
 - base-ten word form (4 ten thousands, 2 thousands, 3 hundreds, 7 tens, and 1 one)
 - number names (forty-two thousand, three hundred seventy-one)
 - expanded form (40,000 + 2,000 + 300 + 70 + 1)
- Understand that when comparing two numbers, one looks at the whole number, not just individual digits
- Understand the role of commas when reading a whole number
- Understand that a number (greater than 0) in the thousands place always has a greater value than the number in the hundreds place
- Line up numbers by place value and describe the place value of each digit to compare the numbers
- Understand that if the number of thousands is the same, the number with more hundreds is greater. If the number of thousands and hundreds is the same, the number with more tens is greater
- Use terms including greater than, more than, less than, fewer than, equal to, and same as, to describe comparisons
- Use the symbols >, =, and < to correctly compare multi-digit numbers

Teacher Notes: Emphasis should be placed on the meaning of quantities rather than tricks such as "the alligator eats the bigger number." The inequality symbols (<, >) are shortcuts for identifying the relationship between two numbers where one is greater or smaller than the other. The statements are read from left to right (for example, 15,000 < 28,000 is read fifteen thousand is less than twenty-eight thousand).

Related Standards: Current Grade Level	Related Standards: Future Grade Levels
4.NBT.1 Recognize that in a multi-digit whole number, a digit in one place	5.NBT.3 Read, write, and compare decimals to thousandths.
represents ten times what it represents in the place to its right.	6.NS.7 Understand ordering and absolute value of rational numbers.
4.NF.7 Compare two decimals to hundredths by reasoning about their size.	Interpret statements of inequality as statements about the relative position
Record the results of comparisons with the symbols >, <, or = and justify the	of two numbers on a number line diagram.
conclusions.	6.EE.8 Write an inequality of the form <i>x</i> > <i>c</i> or <i>x</i> < <i>c</i>

Critical Background Knowledge from Previous Grade Levels

- Compare two fractions with the same numerator or the same denominator. Record the results of comparisons with the symbols >, +, or < (3.NF.3)
- Read and write numbers to 1,000 using base-ten numerals, number names and expanded form (2.NBT.3)
- Compare two three-digit numbers based on meanings of the hundreds, tens, and ones digits, using >, =, and < symbols to record the results of comparisons. (2.NBT.4)
- Understand that the three digits of a three-digit number represent amounts of hundreds, tens, and ones (2.NBT.1)

Academic Vocabulary

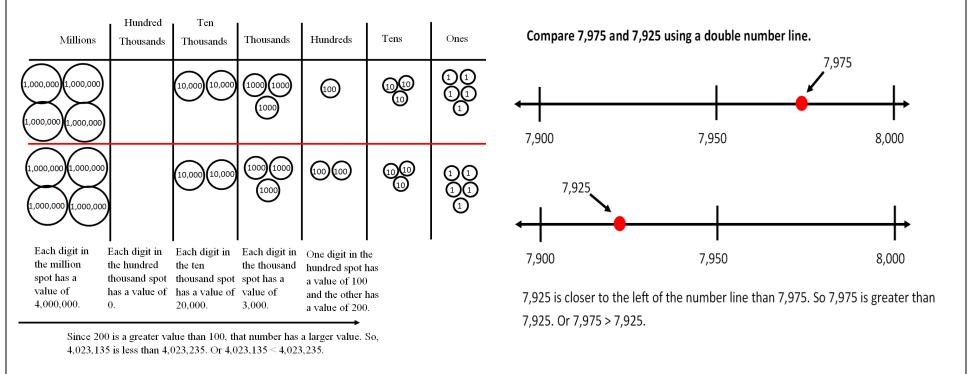
base-ten numeral (formally known as standard form), number names (formally known as word form), expanded form, compare, more, fewer, greater than (>), less than (<), equal to (=), same as

Suggested Strategies

• Use concrete materials such as objects on a place value chart, base-ten blocks, and number lines to compare two multi-digit numbers

Suggested Models

Compare 4,023,135 and 4,023,235 using a place value chart.



Number and Operations in Base Ten Core	Guide	Grade 4
Generalize place value understanding for multi-digit whole numbers by analyze	ing patterns, writing whole numbers in a variety o	f ways, making comparisons,
and rounding (Standards 4.NBT.1–3)		
Standard 4.NBT.3 Use place value understanding to round multi-digit whole r	umbers to any place.	
Concepts and Skills to Master		
Use place value understanding to round whole numbers less than or equ	al to 1,000,000	
• Understand that rounding can be applied to any place within a number		
• Understand when rounding to the nearest tens, hundreds, thousands, te	n-thousands, hundred-thousands, or millions place	, the goal is to approximate
the closest number with zero units in the places to the right of the digit t		the nearest ten-thousand is
480,000; and 478,235 rounded to the nearest hundred-thousand is 500,0	,	
Connect rounding numbers to the location of the number on a number li		
which benchmark number is closer (For example, when rounding 478,23)		
480,000, the midpoint is 475,000. The number 478,235 is to the right of the therefore rounded to 480,000. See the model below)		
Teacher Note: Rounding to the unit represented by the place farthest to the left i	s typically easier for students and often sufficient for	practical purposes Bounding
to the unit represented by a place in the middle of a number may be more difficu		
easier for a student to round 478,235 to 500,000 rather than to 480,000. Student		
Related Standards: Current Course	Related Standards:	
4.NBT.1 Recognize that in a multi-digit whole number, a digit in one place rep		value understanding to round
represents in the place to its right	decimals to hundre	-
4.OA.3 Solve multi-step word problems and assess the reasonableness of ans	wers using mental	
computation and estimation strategies including rounding		
Critical Background Knowledge from Previous Grade Levels	Suggested Model	
Use place value understanding to round two-digit and three-digit numb	ers to the nearest 10 and Example: Round 478,23	35 to the nearest ten thousands.
100 (3.NBT.1)	Step One:	
 Read and write numbers to 1,000 using base-ten numerals, number nar 	ies, and expanded form	E
(2.NBT.3)	unts of hundrods, tons, and	
 Understand that the three-digits of a three-digit number represent amo ones. Understand the value of each digit in three-digit numbers (2.NBT. 		480,000
Academic Vocabulary	Step Two:	
round, benchmark number, midpoint, digit, estimate, close to, nearest place,		i i
thousands place, ten-thousands place, hundred-thousands place, millions place		
Suggested Strategies	470,000	475,000 480,000
 Create and use horizontal and vertical open number lines to identify, local 	te and label benchmark	
numbers, midpoints, and target numbers to assist in rounding	Step Three:	
 Use base-ten blocks to model rounding up to the thousands place 	•	
• Use a place value chart and/or place value disks as a tool for support who	en rounding 470,000	475,000 478,235 480,000
• While songs and mnemonic stories may be engaging, they should not be	used in place of developing	
conceptual understanding of rounding. If these are to be used, they shou	ld come after conceptual Step Four:	
understanding has been developed	•	
 Use drawings to model the concept of rounding 	470,000	475,000 478,235 480,000
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Core Guide

Number and Operations in base ren	Core Guide	Grade 4			
Use place value understanding and prope	erties of operations to perform multi digit addition,	subtraction, multiplication, and division using a one-digit divisor			
(Standards 4.NBT.4–6)					
Standard 4.NBT.4 Fluently add and subtr	act multi-digit whole numbers using the standard a	ılgorithm.			
Concepts and Skills to Master					
Extend understanding of addition ar	nd subtraction of multi-digit whole numbers				
Fluently compute sums and differen	ces of whole numbers using a variety of strategies	including the standard algorithm			
Use properties of operation and place	ce value to explain the standard algorithm				
Build understanding and explain con	nections between various addition and subtraction	ו strategies and the standard algorithm			
Teacher Note: The standard algorithms o	f addition and subtraction are neither an expectati	on nor a focus in second grade. Students use multiple strategies			
for addition and subtraction in grades K-3	By the end of third grade students use a range o	f algorithms based on place value, properties of operations,			
•	-	vhole numbers. Students are expected to fluently add and			
		e. Fourth grade students should not only focus on the standard			
		. "The standards define a computation algorithm as a set of			
	-	when the steps are carried out correctly. In mathematics, an			
		Standards do not specify a particular standard algorithm for			
• • •	ls.me/wp-content/uploads/2015/03/ccss_progress	ion_nbp_k5_2015_03_16.pdf			
Related Standards: Current Grade Level	Related Standards: Future Grade Levels	and using the standard slow other			
4.NBT.1 Recognize that in a multi-digit whole number, a digit in one place	5.NBT.5 Fluently multiply multi-digit whole numbers with up 5.NBT.6 Find quotients of whole numbers with up	o to four-digit dividends and two-digit divisors, using strategies			
represents ten times what it represents		hals to hundredths, using concrete models or drawings and			
in the place to its right	strategies				
	6.NS.3 Fluently add, subtract, multiply, and divid	e multi-digit decimals using the standard algorithm			
Critical Background Knowledge from Previous Grade Levels					
• Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between					
addition and subtraction (3.NBT.2)					
• Fluently add and subtract within 100 using strategies based on place value, properties of operations, and/or the relationship between addition and					
 subtraction (2.NBT.5) Add and subtract within 1,000 using concrete models or drawings (2.NBT.7) 					
Suggested Models		Academic Vocabulary			
1	1 sum, difference, total, addends				
	38				

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{r} 38 \\ + 24 \\ 50 \\ -3 \\ \cancel{5}{5} \\ 3 \\ 6 \\ \cancel{5}{6} \\ -4 \\ \cancel{5}{6} \\ -6 \\ -6 \\ -6 \\ -6 \\ -6 \\ -6 \\ -6 \\ -6$	 sum, difference, total, addends Suggested Strategies Use base ten models and connect the model to the algorithm Connect standard algorithms to strategies for addition and subtraction
Image Source: DSD Advantage Math 4.NBT		

Core Guide

Use place value understanding and properties of operations to perform multi digit addition, subtraction, multiplication, and division using a one-digit divisor (Standards 4.NBT.4–6)

Standard 4.NBT.5 Multiply a whole number of up to four digits by a one-digit whole number, and multiply two two-digit numbers, using strategies based on place value and the properties of operations. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.

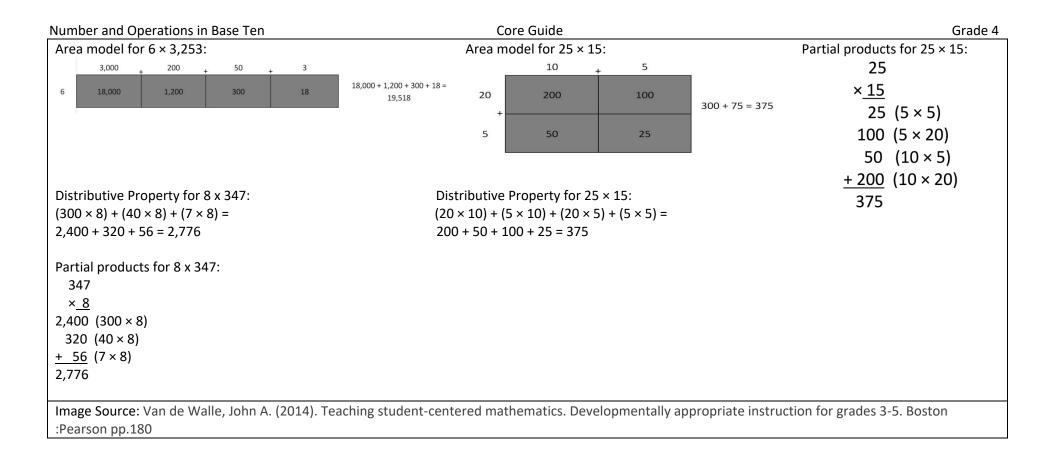
Concepts and Skills to Master

- Extend understanding of multiplication with one-digit numbers to multiply specified multi-digit numbers
- Understand how to compute products of one-digit numbers and multiples of 10, 100, and 1,000
- Use the distributive property to decompose numbers into multiples of 10, 100, and 1,000 and multiply those multiples by one-digit numbers to solve for products
- Explain the pattern when multiplying by a value of 10, 100, or 1,000
- Demonstrate understanding of the relationships between pictures and/or equations representing multiplying whole numbers
- Use a variety of strategies to multiply the following numbers:
 - $\circ~$ one-digit number by a one-digit number
 - one-digit number by a two-digit number
 - o one-digit number by a three-digit number
 - one-digit number by a four-digit number
 - $\circ\;$ two-digit number by a two-digit number

Teacher Note: A standard algorithm of multiplication is <u>neither</u> an expectation nor a focus in fourth grade. Students use multiple strategies for multiplication in grades 3-5. By the end of fourth grade students use a range of algorithms based on place value, properties of operations, and/or the relationships between addition and multiplication to multiply multi-digit whole numbers. Students are expected to fluently multiply multi-digit whole numbers using a standard algorithm by the end of fifth grade.

Related Standards: Current Grade Level	Related Standards: Future Grade Levels
4.OA.2 Multiply or divide to solve word problems involving multiplicative comparison	5.NBT.2 Explain patterns in the number of zeros of the product when
4.OA.3 Solve multi-step word problems posed with whole numbers and having	multiplying a number by powers of 10
whole-number answers using multiplication	5.NBT.5 Fluently multiply multi-digit whole numbers using the
4.OA.4 Find factor pairs and recognize multiples	standard algorithm
4.NBT.1 Recognize that in a multi-digit whole number, a digit in one place represents	5.NBT.7 Multiply decimals to hundredths, using concrete models or
ten times what it represents in the place to its right	drawings and strategies based on place value
4.NBT.6 Find whole-number quotients and remainders with up to four-digit	5.NF.4 Apply and extend previous understandings of multiplication
dividends and one-digit divisors	to multiply a fraction or whole number by a fraction (using area
4.MD.2 Use the four operations to solve measurement word problems	models and partial products)
4.MD.3 Apply the area and perimeter formulas for rectangles in real-world and	6.NS.3 Fluently multiply multi-digit decimals using the standard
mathematical problems	algorithm

Number and Operations in Base Ten	Core Guide		Grade 4
Critical Background Knowledge from Previous Grade Levels			
 Interpret the products of whole numbers, such as interpreting Use multiplication and division within 100 to solve word prob Determine the unknown whole number in a multiplication or Apply properties of operations as strategies to multiply and d Fluently multiply and divide within 100, using strategies such 	blems in situations involving o division equation relating th livide (3.0A.5)	equal groups, arrays, and measu ree whole numbers (3.OA.4)	rement quantities (3.OA.3)
end of third grade, know from memory all products of two orMultiply one-digit whole numbers by multiples of 10 in the radius of the radius	ne-digit numbers (3.OA.7) ange 10–90, for example, 9 ×		operations. By the
 Relate area to the operations of multiplication and addition (a Use addition to find the total number of objects arranged in r to find the total number of squares (2.0A.4, 2.G.2) 		a rectangle into rows and colum	n of same-sized squares and count
Academic Vocabulary			
equal groups, array, area model, multiply, factor, product, factor	r pairs, multiples, distributive	e property, partial products, mu	Itiples of 10, 100, and 1,000
Suggested Strategies			
 Use objects (base-ten blocks or place-value discs) and drawing Write partial product equations to represent arrays and area n Use the distributive property to solve multiplication problems Apply the commutative or associative properties of multiplication 	nodels; Explain connections		-
Suggested Models			
Teacher Note: These models are ordered in a progression from r individual objects to connect to third grade strategies, students Equal groups with groupable objects for $6 \times 34 = 204$: 34 + 34 + 34 + 34 + 34 + 34 = 204	should progress towards mo Equal groups wi		
	=	=" == "	100 4 tens 16
Array with base-ten blocks for 6 × 34 = 204:		Area model with base-ten blocks or graph paper for 16 × 14 = 224:	$6 \text{ tens} \qquad 0 \text{ res} \\ \hline 0 \text{ res} \\ \hline 100 + 40 + 60 + 24 = 224$
4.NBT.5			



Number and Operations in Base Ten

Core Guide

Use place value understanding and properties of operations to perform multi digit addition, subtraction, multiplication, and division using a one-digit divisor (Standards 4.NBT.4–6)

Standard 4.NBT.6 Find whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.

Concepts and Skills to Master

- Extend understanding of division within 100 to divide specified multi-digit numbers by one-digit divisors
- Use a variety of strategies to find quotients between the following numbers with and without remainders:
 - o one-digit divisors and one-digit dividends
 - o one-digit divisors and two-digit dividends
 - one-digit divisors and three-digit dividends
 - o one-digit divisors and four-digit dividends
- Compute quotients in a variety of situations, including with zeros in various places
- Interpret whole-number quotients of whole numbers with and without remainders from partitive and quotative contexts (Partitive: interpret 560 ÷ 8 as the number of objects in each share when 560 objects are partitioned equally into eight shares; Quotative: interpret 560 ÷ 8 as a number of shares when 560 objects are partitioned into equal shares of eight objects each)
- Demonstrate understanding of the relationships between concrete models, pictures, and/or equations
- Understand remainders as the quantity remaining when the divisor does not divide equally into the dividend
- Interpret remainders in relation to standard 4.OA.3

Teacher Note: A standard algorithm of division is neither an expectation nor a focus in fourth grade. There is not just one standard algorithm and students should use multiple strategies for division in grades 3-5. By the end of fourth grade students use a range of algorithms based on place value, properties of operations, and/or the relationships between subtraction and division to divide multi-digit whole numbers. Students are expected to fluently divide multi-digit whole numbers using a standard algorithm by the end of sixth grade.

Related Standards: Current Course	Related Standards: Future Courses
4.OA.2 Multiply or divide to solve word problems involving multiplicative	5.NBT.6 Find whole-number quotients of whole numbers with up to four-
comparison	digit dividends and two-digit divisors
4.OA.3 Solve multi-step word problems posed with whole numbers using the	5.NBT.7 Divide decimals to hundredths
four operations, including problems in which remainders must be interpreted	5.NF.3 Interpret a fraction as division of the numerator by the denominator
4.OA.4 Find factor pairs and recognize multiples	6.NS.2 Fluently divide multi-digit numbers using the standard algorithm
4.NBT.1 Recognize that in a multi-digit whole number, a digit in one place	6.NS.3 Fluently divide multi-digit decimals using the standard algorithm
represents ten times what it represents in the place to its right	
4.MD.2 Use the four operations to solve measurement word problems	

Number and Operations in Base Ten Core Guide Grade 4 Critical Background Knowledge from Previous Grade Levels • Interpret whole-number quotients of whole numbers. For example, interpret 56 ÷ 8 as the number of objects in each share when 56 objects are partitioned equally into eight shares (partitive), or as a number of shares when 56 objects are partitioned into equal shares of eight objects each (quotative) (3.OA.2) • Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities (3.OA.3) • Determine the unknown whole number in a multiplication or division equation relating three whole numbers (3.0A.4) • Apply properties of operations as strategies to multiply and divide (3.OA.5) • Understand division as an unknown-factor problem. Understand the relationship between multiplication and division (multiplication and division are inverse operations). For example, find 32 ÷ 8 by finding the number that makes 32 when multiplied by 8 (3.OA.6) • Fluently multiply and divide within 100, using strategies such as the relationship between multiplication and division or properties of operations. By the end of third grade, know from memory all products of two one-digit numbers (3.OA.7) Multiply one-digit whole numbers by multiples of 10 in the range 10–90, for example, 9 × 80 and 5 × 60 (3.NBT.3) • Use addition to find the total number of objects arranged in rectangular arrays. Partition a rectangle into rows and columns of same-sized squares and count to find the total number of squares (2.OA.4, 2.G.2) Academic Vocabulary dividend, divisor, quotient, equal groups, partial quotients, remainder, place value Suggested Models Connect multiplication to division, area model Equal groups with individual objects for Equal groups with base-ten objects for $206 \div 6 = 34 R 2$ $206 \div 6 = 34 R 2$ for $204 \div 6 = 34$ 30 Remainder 0+20 4+2=6 200 ... 6 -180 $204 \div 6 = 34$ Remainder • Connect multiplication to division, area model for $204 \div 6 = 34$ Array with base-ten blocks for $204 \div 6 = 34$ 30 4 6 180 24 180 + 24 = 204

Number and Operations in Base Ten	Core Guide		Grade 4
How many groups of 5 are in 672? (At least 100) Use 100 as the first partial quotient. $100 \times 5 = 500$ Subtract $672 - 500 = 172$	5/672 100	5/672	
How many groups of 5 are in 172? (At least 20) Use 20 as the second partial quotient. $20 \times 5 = 100$ Subtract $172 - 100 = 72$	/72 /00 20 72	572 100 772	
How many groups of 5 are in 72? (At least 10) Use 10 as the third partial quotient. $10 \times 5 = 50$ Subtract $72 - 50 = 22$	50 10 22 20 4	200 YO 272 200 YO	
How many groups of 5 are in 22? (At least 4) Use 4 as the fourth partial quotient. $4 \times 5 = 20$ Subtract $22 - 20 = 2$	2 134 RZ	72 50 10 22	
Add the partial quotients and record any remainders. 100 + 20 + 10 + 4 = 134 Answer: 134 R2		20 4 2 134 RZ	
Suggested Strategies			
Use the relationship between multiplication and divis			
	 Use repeated subtraction and sharing as division strategies Use manipulatives such as base-ten blocks or place-value discs and drawings such as equal groups, arrays, and area models to represent division 		
	-	quai groups, arrays, and area models to repr	esent division
Use area models and partial quotients to model, expl Simplein expressions between concerns models, micture			
• Explain connections between concrete models, pictur			L D 400 400

Images Source: Van de Walle, John A. (2014). Teaching student-centered mathematics. Developmentally appropriate instruction for grades 3-5. Boston :Pearson pp.180, 189, 190

Number and Operations – Fractions

Core Guide

Extend understanding of equivalence and ordering of fractions (Standards 4.NF.1–2). Denominators for fourth grade are limited to 2, 3, 4, 5, 6, 8, 10, 12, and 100. Standard 4.NF.1 Explain why a fraction a/b is equivalent to a fraction (n x a)/(n x b) by using visual fraction models, with attention to how the number and size

of the parts differ even though the two fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions. Concepts and Skills to Master

- Understand equivalent fractions as the same quantity with different names based on the number and size of the parts
- Recognize and explain how multiplying the numerator and denominator of a fraction by the same number, *n*, corresponds physically to partitioning each unit fraction piece into *n* smaller equal pieces (see model below)
- Explain how the principle of the multiplicative identity property of 1 transforms a fraction into an equivalent fraction and generate equivalent fractions using this principle (Students may, but need not, use the formal term for this property)

Teacher Note: Limit denominators to 2, 3, 4, 5, 6, 8, 10, 12, and 100.

	10013102, 3, 4, 5, 0, 0	, 10, 12, una 100.			
Related Standards: Current Grade Level		Related Standards: Future Grade Levels			
		5.NF.1 and 2 Add and subtract with unlike denominators			
4.NF.3c Replace mixed numbers with equivalent fractions		5.NF.3 Interpret a fraction as division of the numerator by the denominator.		e numerator by the denominator.	
4.NF.5 Express a fraction with denominator 10 as an equivalent fraction		5.NF.5b Relate the principle of fraction equivalence		uivalence	
with denominator 100			6.RP.3 Generate equiva	alent ratios and cor	npare ratios
Critical Background Knowledge from Previous Grade Levels					
 Represent whole numbers as equivalent fractions (3/3 = 1 and 4/1 = 4) (3.NF.3) Understand equivalent fractions as the same quantity with different names (3.NF.3) Denominators are limited to 2, 3, 4, 6, and 8 in third grade Academic Vocabulary 					
Fraction, equivalent fraction	numerator, denomina	ator			
Denominators new to fourth) hundredths $(1/100)$		
Denominators new to rourti	i grade. Intris (75), tenti	13 (1/10), twentis (1/12	<i>j</i> , nunureutiis (1/100)		
Suggested Models Suggested Strategies					
Visual models may include: area of various shapes (circles, rectangles, etc.), bar models, number lines, and double • Use a variety of visual area and					
number lines			the number line to show that		linear fraction models to recognize and generate
		0	1 4/3	2	equivalent fractions.
$\frac{1}{2} \qquad \frac{2}{4} = \frac{2 \times 1}{2 \times 2}$		is also 5×4 p intervals of len	$\frac{1}{3}$ hen each part is $\frac{1}{3}$, and we wa arts when each part is $\frac{1}{5 \times 3}$. ath $\frac{1}{3}$ into 5 parts of equal length ength in the unit interval, and $\frac{4}{3}$	Divide each of the th. There are 5×3	 Explain connections between models and multiplying the numerator and denominator by the same number. Connect visual models to the multiplicative relationships of the
$\frac{1}{2} \qquad \frac{1}{4} \frac{1}{2 \times 2} \qquad \frac{1}{6} \frac{1}{3 \times 2} \qquad \frac{1}{8} \frac{1}{4 \times 2} \qquad parts of equal length in the unit interval, and \frac{4}{3} is 5 \times 4 of these. multiplicative relationships of the numerators and denominators marked by the second denominators in the unit interval of the second denominator is the unit interval of the second denominator in the unit interval of the second denominator is the unit interval of the s$					
	in the second		,p. 06		

Number and Operations – Fractions

Core Guide

100.			
Standard 4.NF.2 Compare two fractions with different numerators and dif	ze that comparisons are valid only when the two fractions refer to the same whole.		
Concepts and Skills to Master			
 that as the number of equal parts being considered (numerator) increated Compare a fraction to a benchmark fraction of 1/2 and 1 whole Compare fractions through creating common numerators, multiplying number multiplied by one remains unchanged) Compare fractions through creating common denominators, multiplying 	o the same whole whole (denominator) increases, the size of the fractional parts decreases and ases, the total amount being considered increases at least one fraction by applying the multiplicative identity property of 1 (any ng at least one fraction by applying the multiplicative identity property of 1		
Teacher Note: While denominators at this grade level are limited to 2, 3, 4, 5, 6, 8, 10, 12, and 100, students may be exposed to other denominators based on strategies used to find common denominators.			
Related Standards: Current Grade Level	Related Standards: Current Grade Level Related Standards: Future Grade Levels		
4.NF.1 Recognize and generate equivalent fractions4.NF.7 Compare two decimals to hundredths by reasoning about their sizes	5.NF.1 and 2 Use equivalent fractions as a strategy to add and subtract fractions6.RP.3 Use ratio and rate reasoning to solve problems		
4.NF.7 Compare two decimals to hundredths by reasoning about their			
4.NF.7 Compare two decimals to hundredths by reasoning about their sizes	6.RP.3 Use ratio and rate reasoning to solve problems nator by reasoning about their size (3.NF.3d)		

Iumber and Operations – Fractions Core Guid	
Suggested Models Suggested Models Students reason using benchmarks such as 1/2 and 1. For example, they see that 7/8 is less than 13/12 because 7/8 is less than 1 (and is therefore to the left of 1 on a number line), but 13/12 is greater than 1 (and is therefore to the right of 1 on a number line). When using the benchmark fraction of $\frac{1}{2}$ to compare $\frac{4}{6}$ and $\frac{5}{8}$ you can use bar models such as these: $\frac{\frac{1}{2} + \frac{1}{6}}{\frac{4}{6}}$ $\frac{\frac{1}{2} + \frac{1}{8}}{\frac{5}{8}}$ $\frac{\frac{1}{2} + \frac{1}{8}}{\frac{5}{8}}$ $\frac{\frac{4}{6} \text{ is } \frac{1}{6} \text{ larger than } \frac{1}{2}, \text{ while } \frac{5}{8} \text{ is } \frac{1}{8} \text{ larger than } \frac{1}{2}. \text{ Since } \frac{1}{6} \text{ is larger than } \frac{1}{8}, \frac{4}{6} \text{ is the greater fraction.}$	 de Grade 4 Suggested Strategies Use a variety of visual fraction models, such as area models and number lines to compare fractions Use benchmark fractions to compare fractions If fractions are the same number of pieces from a whole, compare the size of the missing pieces. This creates opportunities to reason and create common numerators Create equivalent fractions that have common numerators, and then compare the denominators or the size of the fractional parts to compare the fractions (Example: Have students explore ways of comparing 2/3 and 4/5 by finding a common numerator.) Create equivalent fractions that have common denominators, and then compare the numerators or number of parts being considered (Example: have students explore ways of comparing 2/3 and 4/5 by finding a common denominator.)
Area model: The first cake has more left over. The second cake has 5/12 left which is smaller than ½.	
Images Sources: http://commoncoretools.me/wp-content/uploads/2011/08/ccss	progression nf 35 2013 09 19.pdf.
http://www.dpi.state.nc.us/docs/curriculum/mathematics/scos/4.pdf	

Number and Operations – Fractions Core Guide Grad			
Build fractions from unit fractions by applying and extending previous understandings of operations on whole numbers (Standards 4.NF.3–4). Denominators			
for fourth grade are limited to 2, 3, 4, 5, 6, 8, 10, 12, and 100.			
Standard 4.NF.3 Understand a fraction <i>a/b</i> with <i>a</i> >1 as a sum of fractions 1/ <i>b</i> . In other words, any fraction is a sum of unit fractions.			
a. Understand addition and subtraction of fractions as joining and separating parts referring to the same whole.			
b. Decompose a fraction into a sum of fractions with the same denominator in more than one way, recording each decomposition by an equation. Justify			
decompositions, for example, by using a visual fraction model. Fo	or example, 3/8 = 1/8 + 1/8 + 1/8;		
3/8 = 1/8 + 2/8; 2 1/8 = 1 + 1 + 1/8; 2 1/8 = 8/8 + 8/8 + 1/8.			
c. Add and subtract mixed numbers with like denominators, for e	xample, by replacing each mixed number with an equivalent fr	action, and/or by using	
properties of operations and the relationship between addition a	nd subtraction.		
For example, 3 1/4 + 2 1/4 = 13/4 + 9/4 = 22/4; 3 1/4 + 2 1/4 = (3	+ 2) + (1/4 + 1/4) = 5 + 2/4 = 5 2/4, which is equivalent to 22/4.		
d. Solve word problems involving addition and subtraction of fraction of fraction and subtraction of fraction of fraction of fraction of the second	ctions referring to the same whole and having like denominato	rs, for example, by using visua	
fraction models and equations to represent the problem.			
Concepts and Skills to Master			
 Understand and represent that addition and subtraction of fractions with the same denominator is joining or separating parts referring to the same whole 			
• Understand a mixed number is a whole number and a fractio	n that can also be represented as a fraction greater than one		
• Add and subtract fractions with like denominators by replacing each mixed number with an equivalent fraction, and/or by using properties of operations and the relationship between addition and subtraction			
 Solve word problems involving addition and subtraction of fractions with like denominators 			
Teacher Note: All concepts and skills may include fractions greater than one and mixed numbers.			
Related Standards: Current Course	Related Standards: Future Courses		
4.NF.1 Recognize and generate equivalent fractions	5.NF.1 and 2 Use equivalent fractions as a strategy to a		
4.NF.4 Multiply a fraction by a whole number	6.EE.7 Solve real-world and mathematical problems by		
4.NF.5 Add fractions with denominators of 10 and 100	of the form x + a=b for cases in which a, b and x are all r		
4.MD.2 Solve word problems with fraction and decimal numbers4.MD.4 Make a line plot with measurements in fraction units	 6.NS.2–4 Apply and extend previous understandings of rational numbers 	numbers to the system of	

Critical Background Knowledge from Previous Grade Levels

• Understand a unit fraction is a fraction with a numerator of 1 (3.NF.1)

• Understand equivalent fractions (3.NF.3)

• Represent a fraction on a number line (3.NF.2)

Academic Vocabulary

Compose (composition), decompose (decomposition), unit fraction, mixed numbers, fractional form (5/4), fraction greater than one, numerator, denominator

Number and Operations – Fractions	Core Guide Grade 4
Suggested Models	Suggested Strategies
Bar Model 3/8 = 1/8 + 1/8 + 1/8 3/8 = 1/8 + 2/8 3/8 = 1/8 + 2/8	 Use visual fraction models such as number bonds, number lines, fraction strips, bar models, tape diagrams, area models, and rulers to add and subtract fractions with like denominators Connect equations to visual models
$2 \frac{1}{8} = 1 + 1 + \frac{1}{8}$	
Equations (Decompose Fraction)	
$\frac{5}{3} = \frac{3}{3} + \frac{2}{3} = 1 + \frac{2}{3} = 1\frac{2}{3}$	
Number Bond	
$70 - 2\frac{5}{8} = 67\frac{3}{8}$ $67 - 2\frac{8}{8}$	
Number Line	
$\begin{array}{c} 3 \\ 3 \\ 3 \\ 1 \\ 1 \\ 3 \\ 3 \\ 3 \\ 3 \\ 3 \\$	
Images Source: http://www.dpi.state.nc.us/docs/curriculum/mather	matics/scos/4.pdf

Number and Operations - Fractions

fourth grade are limited to 2, 3, 4, 5, 6, 8, 10, 12, and 100.

Build fractions from unit fractions by applying and extending previous understandings of operations on whole numbers (Standards 4.NF.3–4). Denominators for

Standard 4.NF.4 Apply and extend previous understandings of multiplication to multiply a fraction by a whole number. a. Understand a fraction a/b as a multiple of 1/b. For example, use a visual fraction model to represent 5/4 as the product 5 x (1/4), recording the conclusion by *the equation* 5/4 = 5x (1/4). **b.** Understand a multiple of a/b as a multiple of 1/b, and use this understanding to multiply a fraction by a whole number. For example, use a visual fraction model to express $3 \times (2/5)$ as $6 \times (1/5)$, recognizing this product as 6/5. (In general, $n \times (a/b) = (n \times a)/b$). c. Solve word problems involving multiplication of a fraction by a whole number (for example, by using visual fraction models and equations to represent the problem). For example, if each person at a party will eat 3/8 of a pound of roast beef, and there will be five people at the party, how many pounds of roast beef will be needed? Between what two whole numbers does your answer lie? Concepts and Skills to Master • Understand a non-unit fraction (a fraction with a numerator greater than one) as a multiple of a unit fraction and a whole number Represent a repeated addition expression with unit fractions as a multiplication expression with a whole number and a unit fraction • Represent a non-unit fraction in an expression of a unit fraction multiplied by a whole number • Understand a multiple of a non-unit fraction is equivalent to a unit fraction times a whole number $(3x \frac{2}{\pi} as 6x \frac{1}{\pi})$ Solve word problems involving multiplication of a fraction and a whole number Related Standards: Future Grade Levels Related Standards: Current Grade Level **4.NF.2** Utilize benchmark fractions to check for reasonableness of an 5.NF.4 Multiply a fraction by a whole number or fraction **5.NF.6** Solve real-world fraction multiplication problems answer **5.NF.7** Divide unit fractions by whole numbers and whole numbers by unit fractions **4.NF.3** Understand any fraction with a numerator greater than one is the sum of unit fractions **6.EE.7** Solve real-world and mathematical problems by writing and solving equations 4.MD.2 Use multiplication to solve word problems using measurement of the form *ax=b* for cases in which a, b and x are all non-negative rational numbers **6.NS.2–4** Compute fluently with multi-digit numbers; find factors and multiples Critical Background Knowledge from Previous Grade Levels Understand a unit fraction has a numerator of 1 and a non-zero denominator (3.NF.1) • Understand and represent fractions on a number line (3.NF.2) • Interpret the products of whole numbers as the total number of objects in all groups (3.OA.1) • Determine the unknown whole number in a multiplication or division problem (3.OA.4) Academic Vocabulary Unit fraction, multiple, fractional form (5/4), fraction greater than one, mixed number, factor, product, expression, equation, numerator, denominator, whole number 4.NF.4

Number and Operations - Fractions Core Gui	deGrad
Suggested Models	Suggested Strategies
Number Line $0 \frac{1}{6} \frac{2}{6} \frac{3}{6} \frac{4}{6} \frac{5}{6} \frac{6}{6} \frac{7}{6} \frac{8}{6}$ Bar Model $\frac{1}{6} \frac{2}{6} \frac{3}{6} \frac{4}{6} \frac{5}{6} \frac{6}{6}$ $\frac{3}{6} = \frac{1}{6} + \frac{1}{6} + \frac{1}{6} = 3 \times \frac{1}{6}$	 Use a variety of visual fraction models with students when introducing and working with each substandard a, b, and c Build multiplication and repeated addition equations to represent problems Use contexts in word problems when making models to evaluate reasonableness of answers Connect visual models to equations
Each person at a party eats $\frac{2}{5}$ of a pound of meat, and there are 3 people at the party. How many pounds of meat are needed? Between what two	
answers does you answer lie?	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
$3 x_{\overline{5}}^2 = \frac{2}{5} + \frac{2}{5} + \frac{2}{5} = 6 x_{\overline{5}}^1$	
Image Source: http://www.dpi.state.nc.us/docs/curriculum/mathematics/scc	<u>os/4.pdf</u>

Numbers and Operations – Fractions

Core Guide

Understand decimal notation to the hundredths and compare decimal fractions with denominators of 10 and 100 (Standards 4.NF.5–7). Denominators for fourth grade are limited to 2, 3, 4, 5, 6, 8, 10, 12, and 100.

Standard 4.NF.5 Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10 and 100. *For example, express 3/10 as 30/100, and add 3/10 + 4/100 = 34/100.*

Concepts and Skills to Master

- Understand equivalent fractions as the same quantity with different names.
- Add fractions with denominators of 10 and 100
- Create equivalent fractions using Multiplicative Identity Property
- Visualize and create base-ten grids to express a fraction with a denominator of 10 or 100

Teacher Note: Student are first exposed to decimal numbers in fourth grade.

Related Standards: Current Course	Related Standards: Future Courses	
4.NF.1 Equivalent fractions	5.NBT.1 Recognize that in a multi-digit number, a digit in one place	
4.NF.3 Add and subtract fractions with like denominators	represents 10 times as much as it represents in the place to its right and	
4.NF.6 Use decimal notation for fractions with denominators 10 or 100	1/10 of what it represents in the place to its left	
4.NF.7 Compare two decimals to hundredths by reasoning about their size	5.NBT.7 Add, subtract, multiply and divide decimals	
4.MD.2 Solve measurement word problems involving decimals		
Critical Background Knowledge		
 Related Standards: Current Grade Level (see above) 		
 Explain equivalence and generate equivalent fractions (3.NF.3) 		
Academic Vocabulary		
Base-ten fractions, common denominator, equivalent fraction, tenths, hundr	edths	
Suggested Models	Suggested Strategies	
ones . tenths hundredths	 Use strategies that explore equivalent fractions with base-ten blocks, 	
Tenths Grid Hundredths Grid	base-ten grid models, or grid paper	
0.3 = 3 tenths = 3/10 0.30 = 3 hundredths = 3/10		
Image Source: http://www.dpi.state.nc.us/docs/curriculum/mathematics/sco	os/4.pdf	

Understand decimal notation to the hundredths and compare decimal fractions with denominators of 10 and 100 (Standards 4.NF.5–7). Denominators for fourth grade are limited to 2, 3, 4, 5, 6, 8, 10, 12, and 100.

Standard 4.NF.6 Use decimal notation for fractions with denominators 10 or 100. For example, rewrite 0.62 as 62/100, describe a length as 0.62 meters; locate 0.62 on a number line diagram.

Concepts and Skills to Master

- Understand that just as fractions represent part of a whole, decimals represent part of a whole
- Understand that a fraction represented with decimal notation holds the same value as the fraction
- Identify the digit to the right of the decimal point as the tenths place and the digit two places to the right of the decimal point at the hundredths place

Teacher Note: Being precise with language when saying decimals is important. For example, always say "five and two tenths", rather than "five point two." When teachers and students are precise with their language it will provide an opportunity for students to hear the connection between fractions and decimals (Van De Walle, 2014).

Related Standards: Current Course	Related Standards: Future Courses	
4.NF.5 Express equivalent fractions with denominators of 10 and 100	5.NBT.1 Recognize digits in places as 10 times as much as places to the right,	
4.NF.7 Compare two decimals to hundredths by reasoning about their size	and 1/10 as much as places to the left	
4.MD.2 Solve measurement problems using simple decimals	5.NBT.3 Read, write, and compare decimals to thousandths	
	5.NBT.7 Add, subtract, multiply, and divide with decimals	

Critical Background Knowledge from Previous Grades

• Understand that the three digits of a three-digit number represent amounts of hundreds, tens, and ones (2.NBT.1)

Academic Vocabulary

tenths, hundredths, decimal, equivalent fraction, decimal notation

Suggested Models	Suggested Strategies
Hundreds Tens Ones • Tenths Hundredths • 3 2	 Relate fractions and decimals as the same value by using visual models such as base ten blocks and grids, number lines, meter sticks, place value chart and money
Images Source: http://www.dpi.state.nc.us/docs/curriculum/mathematics/s	<u>icos/4.pdf</u>

Numbers and Operations – Fractions

Core Guide

	Understand decimal notation to the hundredths and compare decimal fractions with denominators of 10 and 100 (Standards 4.NF.5–7). Denominators for		
fourth grade are limited to 2, 3, 4, 5, 6, 8, 10, 12, and 100.			
Standard 4.NF.7 Compare two decimals to hundredths by reasoning about their size. Recognize that comparisons are valid only when the two decimals refer			
to the same whole. Record the results of comparisons with the symbols >, =, or <, and justify the conclusions, for example, by using a visual model.			
Concepts and Skills to Master			
 Understand comparisons are only valid when the two fractions or decimals refer to the same whole 			
Compare decimals by reasoning that as the number of equal parts in a whole increases, the size of the fractional parts decreases (hundredths are			
smaller than tenths)			
Extend place value understanding to tenths and hundredths			
Create and compare base-ten grids to express a fraction with a denomination			
Related Standards: Current Course	Related Standards: Future Courses		
4.NBT.2 Read, write, and compare multi-digit whole numbers	5.NBT.1 Recognize digits in places as 10 times as much as places to the right,		
4.NF.2 Compare fractions with different numerators and denominators 4.NF.6 Use decimal notation for fractions with denominators 10 or 100	and 1/10 as much as places to the left 5.NBT.3 Read, write, and compare decimals to the thousandths		
	5.NBT.5 Read, write, and compare decimals to the thousandths		
Critical Background Knowledge from Previous Grade Levels			
• Compare two fractions with the same numerator or the same denominator by reasoning about their size (3.NF.3d)			
Compare two three-digit numbers (2.NBT.4)			
Academic Vocabulary			
decimal, tenth, hundredth, equivalent, >, =,<, compare,			
Suggested Models	Suggested Strategies		
Suggested Models Seeing that 0.2 > 0.09 using a visual	Relate and compare fractions and decimals as the same value by using		
Suggested Models	 Relate and compare fractions and decimals as the same value by using visual models such as base ten blocks and grids, number lines, meter 		
Suggested Models Seeing that 0.2 > 0.09 using a visual	Relate and compare fractions and decimals as the same value by using		
Suggested Models Seeing that 0.2 > 0.09 using a visual	 Relate and compare fractions and decimals as the same value by using visual models such as base ten blocks and grids, number lines, meter 		
Suggested Models Seeing that 0.2 > 0.09 using a visual	 Relate and compare fractions and decimals as the same value by using visual models such as base ten blocks and grids, number lines, meter 		
Suggested Models Seeing that 0.2 > 0.09 using a visual	 Relate and compare fractions and decimals as the same value by using visual models such as base ten blocks and grids, number lines, meter 		
Suggested Models Seeing that 0.2 > 0.09 using a visual	 Relate and compare fractions and decimals as the same value by using visual models such as base ten blocks and grids, number lines, meter 		
Suggested Models Seeing that 0.2 > 0.09 using a visual	 Relate and compare fractions and decimals as the same value by using visual models such as base ten blocks and grids, number lines, meter 		
Suggested Models Seeing that 0.2 > 0.09 using a visual fraction model	 Relate and compare fractions and decimals as the same value by using visual models such as base ten blocks and grids, number lines, meter 		
Suggested Models Seeing that 0.2 > 0.09 using a visual fraction model The shaded region on the left shows 0.2 of the	 Relate and compare fractions and decimals as the same value by using visual models such as base ten blocks and grids, number lines, meter 		
Suggested Models Seeing that 0.2 > 0.09 using a visual fraction model The shaded region on the left shows 0.2 of the unit square, since it is two parts when the square	 Relate and compare fractions and decimals as the same value by using visual models such as base ten blocks and grids, number lines, meter 		
Suggested Models Seeing that 0.2 > 0.09 using a visual fraction model Image:	 Relate and compare fractions and decimals as the same value by using visual models such as base ten blocks and grids, number lines, meter 		
Suggested Models Seeing that 0.2 > 0.09 using a visual fraction model Image:	 Relate and compare fractions and decimals as the same value by using visual models such as base ten blocks and grids, number lines, meter 		
Suggested Models Seeing that 0.2 > 0.09 using a visual fraction model Image:	 Relate and compare fractions and decimals as the same value by using visual models such as base ten blocks and grids, number lines, meter 		

Solve problems involving measurement and conversion of measurements from a larger unit to a smaller unit (Standards 4.MD.1–2)			
Standard 4.MD.1 Know relative sizes of measurement units within each system of units (standard and metric), including kilometers, meters, and centimeters;			
liters and milliliters; kilograms and grams; pounds and ounces; hours, minutes,	and seconds. Within a single system of measurement, express measurements		
in a larger unit in terms of a smaller unit. Record measurement equivalents in a	two-column table. For example, know that one foot is 12 times as long as one		
inch. Express the length of a four-foot snake as 48 inches. Know that one meter is 100 times as long as one centimeter. Generate a conversion table for feet			
and inches listing the number pairs (1, 12), (2, 24), (3, 36)			
Concepts and Skills to Master			
Know relative sizes of measurement units using benchmarks and mental images of units introduced in previous grades (see Critical Background			
Knowledge below) and units new to fourth grade (kilometers, pounds, ounces, and seconds)			
• Understand that a given measurement can be expressed using different units, yet retain the same value (1 ft. can be represented as 12 in. without			
altering the value; 1 ft. = 12 in.)			
 Generalize the relationship between larger and smaller units (1 foot is 12 times as long as one inch) 			
 Convert/Express larger units in terms of smaller units within the same system of measurement using multiplication (converting smaller units to larger units using division begins in fifth grade) 			
quarts, and gallons. Students should not be expected to memorize unit conversions; however, knowing relative sizes of measurement units within systems of units and having repeated exposure to commonly used units will support them in being able express measurements in a larger unit in terms of a smaller unit. The core standards do not differentiate between weight and mass. Technically, mass is the amount of matter in an object. Weight is the force exerted on the body of gravity. On the earth's surface, the distinction is not important. Therefore, mass and weight may be used interchangeably in solving measurement problems related to the standard.			
Related Standards: Current Grade Level	Related Standards: Future Grade Levels		
4.MD.2 Solve word problems involving distances, intervals of time, liquid	5.MD.1 Use unit conversions in solving multi-step, real world problems		
volumes, masses of objects, and money	6.RP.3.d Use ratio reasoning to convert measurement units; manipulate and		
4.OA.1 Interpret a multiplication equation as a comparison	transform units appropriately when multiplying or dividing quantities		
4.OA.2 Multiply to solve word problems involving multiplicative comparison			
Critical Background Knowledge			
 Distances: Measure lengths with halves and fourths of an inch (3.MD.4); Estimate, measure, add, and subtract lengths using inches, feet, yards, centimeters, and meters (2.MD.1-6) 			
• Liquid Volumes: Measure and estimate masses of objects using grams and kilograms and liquid volumes using milliliters and liters (3.MD.2)			
• Masses of objects: Measure and estimate; add, subtract, multiply, or divide to solve one-step word problems given the same units (3.MD.2)			
• Time: Tell and write time to the nearest minute. Add and subtract time intervals in minutes using number line diagrams (3.MD.1); Tell and write time to the nearest 5 minutes using a.m. and p.m. (2.MD.7)			

Academic Vocabulary Distances: metric system, distance, length, Kilometer (km), meter (m), centimeter (cm), standard/customary system, mile (mi.), yard (yd.) feet (ft.) inch (in.) Liquid volumes: liquid volume, capacity, liter (I), milliliter (mI), gallon (gal.), quart (qt.), pint (pt.), cup (c.), fluid ounce (fl. oz.) Masses of objects: mass, weight, kilogram (kg), gram (g), pound (lb.), ounce (oz.) Time: hour (hr.), minute (min.), second (sec.) Suggested Models Suggested Strategies • Measure the same object using two different units, then compare the measurements to the size of the units being used 3 feet • Draw pictures and models to generalize conversions (see the feet inches 1 foot 1 foot 1 foot image to the left) 1 12 • Create a two-column chart or table to notice any patterns for 2 24 converting within given measurements (see the table to the left) 3 36 36 inches 4 48 feet 5 60 6 72 12 13 14 15 16 17 18 19 20 21 22 23 24 25 7 84 inches

Solve problems involving measurement and conversion of measurements from a larger unit to a smaller unit (Standards 4.MD.1–2)				
Standard 4.MD.2 Use the four operations to solve word problems involving distances, intervals of tim	ne, liquid volumes, masses of objects, and money.			
a. Include problems involving simple fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller				
unit.				
b. Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale.				
Concepts and Skills to Master				
Know relative sizes of measurement units using benchmarks and mental images of units introduced in previous grades (see Critical Background				
Knowledge below) and units new to fourth grade (kilometers, pounds, ounces, and seconds)				
 Add, subtract, multiply, or divide with whole numbers to solve word problems involving measurement units 				
 Express larger units in terms of smaller units 				
• Add simple decimals including tenths and hundredths in which the sum of the two decimals is less than or equal to 0.99 and NO composing across place				
values (regrouping) is required (0.5 + 0.4 = 0.9; 0.25 + 0.3 = 0.55). (Students are not expected to operate with decimals outside of these parameters until				
5th grade. In 4.NF.5, students add fractions with denominators 10 and 100. In 4.NF.6, students express fractions with denominators 10 and 100 using				
decimal notation.)				
 Use decimal notation to represent money (\$0.75 is another notation for 75¢) Add and subtract simple fractions with like denominators including denominators of 2, 2, 4, 5, 6, 8, 10, 12, or 100 (see 4 NF 2). 				
 Add and subtract simple fractions with like denominators including denominators of 2, 3, 4, 5, 6, 8, 10, 12, or 100 (see 4.NF.3) Maccurations intervals (classed time) and called used are blance involving addition and cubits time intervals using barrier minutes and called used time). 				
• Measure time intervals (elapsed time) and solve word problems involving addition and subtraction of time intervals using hours, minutes, and seconds				
Teacher Note: Students combine competencies from other Strands (Numbers and Operations-Fractions, etc.) to solve measurement problems. The Core				
Standards do not have an exhaustive list of measurement units students work with. Students should a				
listed in the Core Standards: millimeters, miles, fluid ounces, cups, pints, quarts, and gallons. Student				
conversions; however, knowing relative sizes of measurement units within systems of units and havir	ng repeated exposure to commonly used units will			
support them in being able express measurements in a larger unit in terms of a smaller unit.				
Related Standards: Current Grade Level	Related Standards: Future Grade Levels			
4.MD.1 Know relative sizes of measurement units and express units in a larger unit in terms of a	5.MD.1 Use unit conversions in solving multi-step, real			
smaller unit using a two-column table	world problems			
4.OA.3 Solve multi-step word problems using the four operations	5.NF.5 Interpret multiplication as scaling			
4.NF.3 Add and subtract fractions with like denominators	6.RP.2 Understand and use unit rates in the context of			
4.NF.4 Multiply a fraction by a whole number	ratio relationships			
4.NF.5 Add fractions with denominators of 10 and 100				
4.NF.6 Use decimal notation for fractions with denominators 10 or 100				
Critical Background Knowledge				
• Distances: Measure lengths with halves and fourths of an inch (3.MD.4); Estimate, measure, add, and subtract lengths using inches, feet, yards,				
centimeters, and meters (2.MD.1-6)				
 Liquid Volumes: Measure and estimate masses of objects using grams and kilograms and liquid volumes using milliliters and liters (3.MD.2) Masses of objects: Measure and estimate; add, subtract, multiply, or divide to solve one-step word problems given the same units (3.MD.2) 				
 Masses of objects: Measure and estimate; add, subtract, multiply, or divide to solve one-step word problems given the same units (3.MD.2) Intervals of time: Tell and write time to the nearest minute. Add and subtract time intervals in minutes using number line diagrams (3.MD.1); Tell and write 				
time to the nearest 5 minutes using a.m. and p.m. (2.MD.7)				
 Money: Solve word problems involving dollar bills, quarters, dimes, nickels, and pennies using \$ and \$ symbols (2.MD.8); Identify the value of pennies, 				
nickels, dimes and quarters (1.MD.5)				

Academic Vocabulary	
Distances: metric system, distance, length, Kilometer (km), meter (m), ce feet (ft.) inch (in.) Intervals of time: elapsed time, time interval, hour (hr.), minute (min.), se Liquid volumes: liquid volume, capacity, liter (l), milliliter (ml), gallon (gal Masses of objects: mass, weight, kilogram (kg), gram (g), pound (lb.), our Money: value, dollar (\$), cent (¢)	.), quart (qt.), pint (pt.), cup (c.), fluid ounce (fl. oz.)
Suggested Models	Suggested Strategies
Use number line diagrams to solve word problems Juan spent 1/4 of his money on a game. The game cost \$20. How much money did he have at first? ? 0 10 20 30 40 50 60 70 80 90 What time does Marla have to leave to be at her friend's house by a quarter after 3 if the trip takes 90 minutes?	 Solve measurement word problems including operations of addition, subtraction, multiplication, and division using visual models including number lines, base ten blocks, and drawings Create a two-column chart or table to notice any patterns for converting within given measurements Use number line diagrams to solve word problems
90 minutes 1:30 1:45 2:00 2:15 2:30 2:45 3:00 3:15 3:30 Using a number line diagram to represent time is easier if stu- dents think of digital clocks rather than round clocks. In the latter case, placing the numbers on the number line involves consider- ing movements of the hour and minute hands. Image Source: https://commoncoretools.files.wordpress.com/2012/07/c	

Measurement and Data	Core Guide Gr	ade 4
Apply knowledge of area and perimeter to solve real world and mathe	ematical problems (Standard 4.MD.3)	
Standard 4.MD.3 Apply the area and perimeter formulas for rectangle	es in real-world and mathematical problems. <i>For example, find the width of a rectang</i>	jular
room given the area of the flooring and the length, by viewing the area	a formula as a multiplication equation with an unknown factor.	
Concepts and Skills to Master		
 Apply the area formula to solve real world problems 		
 Apply the perimeter formula(s) to solve real world problems 		
• Understand the meaning of and solve for variables in area and period	meter formulas	
Teacher Note: "'Apply the formula' does not mean write down a mem	norized formula and put in known values Working with perimeter and area of	
rectangles is still grounded in specific visualizations and numbers E	By repeatedly reasoning about constructing situation equations for perimeter and are	еа
involving specific numbers and an unknown number, students will bui	ild a foundation for applying area, perimeter, and other formulas by substituting spec	cific
values for the variables in later grades." (https://commoncoretools.file	les.wordpress.com/2012/07/ccss_progression_gm_k5_2012_07_21.pdf, p. 22)	
Related Standards: Current Course	Related Standards: Future Courses	
4.NBT.4 Fluently add and subtract multi-digit whole numbers	5.MD.5 Relate volume to the operations of multiplication and addition and set	olve
4.NBT.5 Multiply a whole number of up to four digits by a one-digit w		
number and multiply two two-digit numbers 4.OA.3 Solve multi-step word problems with whole numbers	6.G.1 Find the area of right triangles, other triangles, special quadrilaterals, a polygons by composing and decomposing into rectangles, triangles and /or ot	
4.0A.3 Solve multi-step word problems with whole numbers	shapes; apply these techniques in the context of solving real-world problems	.ner
Critical Background Knowledge from Previous Grade Levels	shapes, apply these teening des in the context of solving real world problems	
	s of polygons, including finding the perimeter given the side lengths, finding an unkno	
	d different areas or with the same area and different perimeters (3.MD.8)	
 Relate area to the operations of multiplication and addition (3.MD 	, , , ,	
• Use multiplication and division within 100 to solve real-world prob		
• Determine the unknown whole number in a multiplication or divis	sion equation relating three whole numbers (3.OA.4)	
• Solve two-step word problems using the four operations using wh	ole numbers (3.OA.8)	
Academic Vocabulary		
rectangle, perimeter, area, array, unit, square units, rectangular perim	neter formula (P = 2I + 2w), rectangular area formula (A = I x w)	
Suggested Models	Suggested Strategies	
	 Use graph paper or square tiles to make a rectan 	igle
	with no gaps or overlaps, then count the square	
32 ft. ² 4ft. of carpet	units to find the area. Count the side lengths to f	ind
32 ft. ² 4 ft. of carpet	the perimeter. Compare these strategies to the	
	formulas. • Solve word problems given an area and one side	
	length by finding the unknown side	
ft.	Read and discuss measurement word problems t	to
	ering the miniature golf course identify when to solve for perimeter or area; solve for perimeter or ar	
	. How many 1-foot squares of the problems using models and diagrams	
carpet will he need to	cover the entire course?	
What is the perimeter		
Image Source: http://www.dpi.state.nc.us/docs/curriculum/mathema	atics/scos/4.pdf	

Represent and interpret data through the use of a line plot (Standard 4.MD.4)

Standard 4.MD.4 Make a line plot to display a data set of measurements in fractions of a unit (halves, quarters, and eighths). Solve problems involving addition and subtraction with like denominators of fractions by using information presented in line plots. *For example, use a line plot to find and interpret the difference in length between the longest and shortest pencils in a classroom.*

Concepts and Skills to Master

• Make a line plot using provided data sets; include a horizontal scale, title, labels, and straight columns of symbols to represent the data points (• or X)

• Use a variety of strategies to solve addition and subtraction problems related to data on a line plot

Teacher Note: In fourth grade students are not expected to generate measurement data. However, third grade students only measure to the fourth of an inch. This standard is an appropriate place for students to learn to measure to the eighth of an inch.

Related Standards: Current Grade Level	Related Standards: Future Grade Levels
 4.MD.2 Use the four operations to solve word problems, including simple fractions and represent measurement quantities using diagrams 4.NF.1 Explain why fractions are equivalent and generate equivalent fractions 4.NF.3c Add and subtract mixed numbers with like denominators 	 5.MD.2 Make line plots with measurements to the half, quarter, and eighth of a unit. Solve problems involving operations of fractions. 5.NF.2 Solve real world problems involving the addition and subtraction of fractions referring to the same whole, including cases of unlike denominators

Critical Background Knowledge from Previous Grade Levels

• Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show the data by making a line plot where the horizontal scale is marked off in appropriate units-whole numbers, halves, or quarters (3.MD.4)

- Understand line plots represent measurement data, not categorical data (3.MD.3, 3.MD.4)
- Generate measurement data and make line plots using whole number units (2.MD.9)

Academic Vocabulary

line plot, fraction, measurement, data, data set, unit

Suggested Models	Suggested Strategies
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	 Generate ideas about what measurement data could be generated and represented on a line plot Measure physical objects or distances varying in length; use data to create a line plot Students may use tally marks or data tables to record measurements prior to creating a line plot or they may produce the line plot as the data are being collected

Measurement and Data Core Guide	Grade 4
Understand various concepts of angles and angle measurement (Standard 4.MD.5–	7).
Standard 4.MD.5 Recognize angles as geometric figures that are formed wherever the measurement.	
a. Understand that an angle is measured with reference to a circle with its center at circular arc between the points where the two rays intersect the circle. An angle that used to measure other angles.	at turns through 1/360 of a circle is called a "one-degree angle," and can be
b. Understand that an angle that turns through <i>n</i> one-degree angles is said to have Concepts and Skills to Master	an angle measure of n degrees.
 Understand that angles are measured with reference to a circle with its center at 	the common endpoint of the ray
 Understand that the arc between the points where the rays intersect is a fraction 	
 Recognize angles as geometric figures that are formed wherever two rays share a 	
 Understand that a one-degree angle means the angle has turned 1/360 of a circle 	
• Understand that the number of one-degree angles an angle turns through is the	
Teacher Note: This standard brings up a connection between angles and circular me	
and become familiar with half-circle protractors (physical and digital) with the numl	bers going in both directions.
Related Standards: Current Grade Level	Related Standards: Future Grade Level
4.MD.6 Measure angles in whole-number degrees using a protractor	7.G.2 Construct triangles from three measures of angles
4.MD.7 Recognize angle measures as additive and solve to find unknown angles	7.G.5 Use facts about supplementary, complementary, vertical, and
4.G.1 Draw and identify lines and angles	adjacent angles in a multi-step problem to write, and use them to solve
4.G.2 Classify two-dimensional figures based on lines and angles	simple equations for an unknown angle in a figure
Critical Background Knowledge from Previous Grade Levels	
 Students recognize the number of angles in shapes in previous grade levels, but r 	measuring angles is not addressed in previous grades
 Understand that shapes in different categories may share attributes (3.G.1) 	
Recognize and draw shapes having specified attributes, such as a given number of	of angles (2.G.1)
Academic Vocabulary	
circular arc, angle, vertex, circle, ray, degree, degree symbol (⁰), endpoint, one-degr	ee, 360°, center, fraction
Suggested Models	Suggested Strategies
Pose the question: A water sprinkler rotates one-degree at each interval. If the sprinkler rotates a total of 100°, how many one-degree turns has the sprinkler made? An angle An angle Iname measurement right angle 90° straight angle 180° acute angle between 0 and 90° obtuse angle between 90° and 180° reflex angle between 180° and 360°	 Connect prior knowledge of clocks to the concept of 360° in a circle Use arms to make angles Use a variety of manipulatives to demonstrate angle rotations for example licorice, cardboard and brad fastener, straws, clay, etc. Find, identify, and discover examples of angles in the classroom or environment
Image Source: Advantage Math Davis School District, https://www.cgcs.org/cms/lib/DC	00001581/Centricity/Domain/120/ccss_progression_gm_k5_2012_07_21.pdf

andard 4.MD.6 Measure angles in whole-number degrees using a protrac oncepts and Skills to Master Understand how use a protractor to measure angles Measure angles in whole-number degrees with a protractor	tor. Sketch angles of specified measure.
Understand how use a protractor to measure angles	
Measure angles in whole-number degrees with a protractor	
Sketch angles of specified measures with a protractor	
Understand benchmark angles: 0°,45° [,] 90° , 180°, 360°	
Read notation to name angles ∠ABC	
Read different notations of angle measures (90° is the same as \Box)	
at a 360° rotation about a point makes a complete circle to recognize and nderstanding to recognize and sketch angles that measure approximately a	ey need experience with benchmark angles. They transfer their understanding sketch angles that measure approximately 90 ⁰ and 180 ⁰ . They extend this 45° and 30°. In fourth grade students should be exposed to and become familiar both directions. Students are only required to read the angle notation, ∠ABC, not
elated Standards: Current Grade Level	Related Standards: Future Grade Level
G.1 Draw and identify lines and angles	7.G.2 Construct triangles from three measures of angles
G.2 Classify shapes by properties of their lines and angles	7.G.5 Use facts about supplementary, complementary, vertical, and adjacent
MD.5 Recognize and understand angles in reference to a circle	angles in a multi-step problem to write, and use them to solve simple equations
MD.7 Recognize angle measures as additive and solve to find unknown ngles	for an unknown angle in a figure
.0	
itical Background Knowledge from Previous Grade Levels	
Students recognize the number of angles in shapes in previous grade leve	
Understand that shapes in different categories may share attributes (3.G	.1)
Recognize and draw shapes having specified attributes, such as a given n	umber of angles (2.G.1)
cademic Vocabulary	
ngle, ∠ABC, degree, degree symbol (°), ray, protractor, acute, and obtuse,	benchmark angles: 0°,45° [,] right 🗆 90°, straight 180°, circle 360°

Core Guide

Grade 4

Measurement and Data

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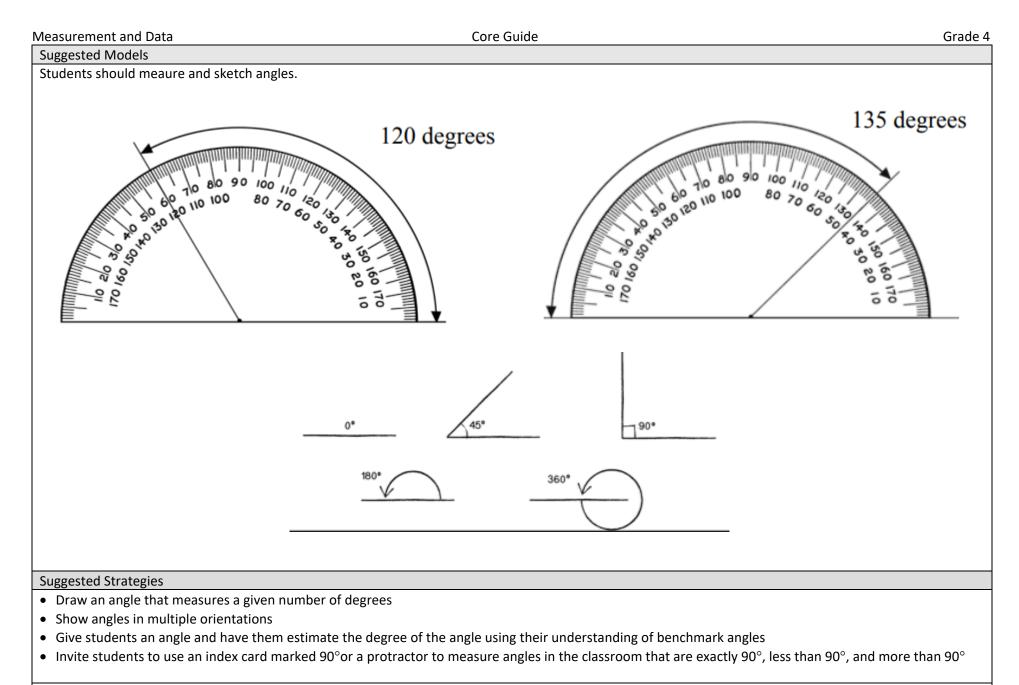


Image Source: http://www.dpi.state.nc.us/docs/curriculum/mathematics/scos/4.pdf

Measurement and Data	Core Gui	de Grade 4	
Understand various concepts of angles and angle measurement (Standard 4.MD.5–7).			
Standard 4.MD.7 Recognize angle measure as additive.			
a. Understand that when an angle is decomposed into non-overlapping parts, the angle measure of the whole is the sum of the angle measures of the parts.			
	on a diagrai	m in real-world and mathematical problems, for example by using an equation	
with a symbol for the unknown angle measure.			
Concepts and Skills to Master			
 Understand two non-overlapping (adjacent) angles can be added 	together to	o find the sum of both angles	
 Recognize angle measure as additive 			
• Solve addition and subtraction problems to find unknown angles	in real-worl	ld situations	
Teacher Note: Students are only required to read the angle notation	n, ∠ABC, nc	ot create it. Angles labeled with measures are not always drawn to scale.	
Related Standards: Current Grade-Level Related Standards: Future Grade-Levels			
4.MD.5 Recognize and understand angles in reference to a circle 7.G.2 Construct triangles from three measures of angles			
4.MD.6 Measure angles in whole-number degrees using a 7.G.5 Use facts about supplementary, complementary, vertical, and adjacent angle			
protractor multi-step problem to write, and use them to solve simple equations for an unknow			
angle in a figure			
Critical Background Knowledge from Previous Grade Levels			
Students recognize the number of angles in shapes in previous gr		but measuring angles is not addressed in previous grades	
Understand that shapes in different categories may share attribu	. ,		
Recognize and draw shapes having specified attributes, such as a			
Use addition and subtraction within 100 to solve one- and two-st	• •	oblem (2.0A.1)	
 Find the unknown whole number using addition and subtraction 	(1.0A.8)		
Academic Vocabulary			
additive, decompose, non-overlapping (adjacent), angle, sum, degre	ee, degree s	symbol °, acute angle, obtuse angle, straight angle, right angle, angle measure,	
perpendicular			
Suggested Models		Suggested Strategies	
$\begin{array}{c} 20^{\circ} \\ 90^{\circ} \\ \hline \\ 180 - (90 + 20) = ? \\ 180 - 110 = 70^{\circ} \end{array}$	res 90°.	 Solve problems such as the following: A lawn water sprinkler rotates 50 degrees and then pauses. It then rotates an additional 25 degrees. What is the total degrees the sprinkler has rotated? If the water sprinkler rotates a total of 25 degrees then pauses. How many 25 degree cycles will it go through for the rotation to reach at least 90 degrees? 	
Image Source: http://www.dpi.state.nc.us/docs/curriculum/mathen	natics/scos	/4.pdf	

Geometry

Draw and identify lines and angles, as well as classify shapes by properties of their lines and angles (Standards 4.G.1–3).

Standard 4.G.1 Draw points, lines, line segments, rays, angles (right, acute, and obtuse), and perpendicular and parallel lines. Identify these in twodimensional figures.

Concepts and Skills to Master

- Draw points, lines, line segments, rays, angles (right, acute, and obtuse), perpendicular and parallel lines
- Identify points, lines, line segments, rays, angles (right, acute, and obtuse), perpendicular and parallel lines in two-dimensional figures

Teacher Note: In third grade students informally recognize attributes of quadrilaterals, including parallel lines and right angles. Although students need to develop explicit awareness of and vocabulary for many concepts they have been developing, including points, lines, line segments, rays, angles (right, acute, obtuse), and perpendicular and parallel lines, it is more important that they construct examples of these concepts. For example, drawing angles and triangles that are acute, obtuse, and right, will help students form a richer conceptual understanding of how these images are connected to their verbal definitions. (http://commoncoretools.me/wp-content/uploads/2014/12/ccss_progression_gk6_2014_12_27.pdf)

Related Standards: Current Grade Level	Related Standards: Future Grade Levels
4.G.2 Classify two-dimensional figures based on the presence or absence	5.G.3 Understand that attributes belonging to a category of two-dimensional
of parallel or perpendicular lines, or the presence or absence of angles of a	figures all belong to all subcategories of that category
specified size. Recognize right triangles as a category, and identify right	5.G.4 Classify two-dimensional figures in a hierarchy based on properties
triangles	
4.MD.5 Recognize angles as geometric figures that are formed wherever	
two rays share a common endpoint, and understand concepts of angle	
measurement	
Critical Background Knowledge from Previous Grade Levels	

Critical Background Knowledge from Previous Grade Levels

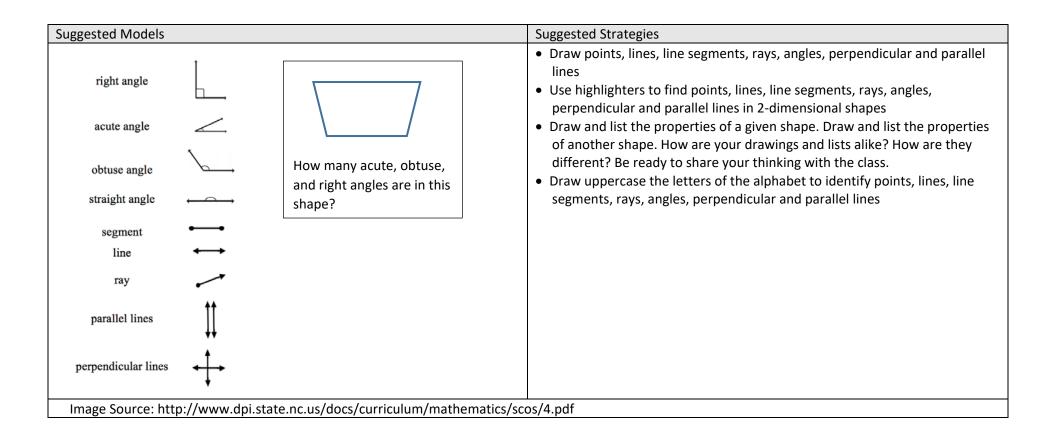
• Understand that shapes in different categories may share attributes, and that the shared attributes can define a larger category. Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories (3.G.1)

- Recognize and draw shapes having specified attributes, such as a given number of sides of angles. Identify and describe quadrilaterals, squares, rectangles, and trapezoids (2.G.1)
- Identify and distinguish between defining attributes versus non-defining attributes; build and draw shapes that possess defining attributes (1.G.1)
- Students work with trapezoids, squares, rectangles, triangles, circles, and hexagons in first and second grade. The term *quadrilateral* is introduced in second grade. Rhombuses and parallelograms are introduced in third grade.

Academic Vocabulary

point, line, line segment, ray, angle (\angle), obtuse, acute, right, parallel (\parallel), perpendicular (\perp), two-dimensional, figure, attribute, angle, closed figure, faces,
polygon, rhombus, rectangle, side, square, parallel, parallelogram, quadrilateral, trapezoid, vertex, right angle (🟳)

Teacher Note: Rectilinear figures must have four right angles. Ensure that correct plural forms of vocabulary words are used. The plural form for rhombus may be rhombuses or rhombi (may be used interchangeably). The plural form for vertex is vertices.



ometry Core Guide Grad		
Draw and identify lines and angles, as well as classify shapes by properties of their lines and		
angles (Standards 4.G.1–3)		
Standard 4.G.2 Classify two-dimensional figures based on the presence or absence of parallel or perpendicular lines, or the presence or absence of angles of a		
specified size. Recognize right triangles as a category, and identify right triangles.		
Concepts and Skills to Master		
 Classify two-dimensional figures based on the presence or absence of parallel or perpendicular lines 		
Classify two-dimensional figures based on the presence or absence of angles	of a specified size	
• Identify right triangles (any triangle with an angle measuring 90 degrees).		
• Use side length to classify triangles as equilateral, equiangular, isosceles, or s	scalene	
 Use angle size to classify them as acute, right, or obtuse 		
Teacher Note: Students may be exposed to the terms equilateral, isosceles, and scalene to describe triangles.		
Related Standards: Current Grade Level Related Standards: Future Grade Levels		
4.G.1 Understand that shapes in different categories may share attributes ,	5.G.3 Understand that attributes belonging to a category of two-dimensional statements of the statement of	onal
and that the shared attributes can define a larger category	figures all belong to all subcategories of that category.	Jilai
4.MD.5 Recognize angles as geometric figures that are formed wherever two	5.G.4 Classify two-dimensional figures in a hierarchy based on properties.	•
rays share a common endpoint, and understand concepts of angle	G.6.1 Students need to identify right triangles	
measurement	, , , , , , , , , , , , , , , , , , , ,	
4.MD.6 Measure angles in whole-number degrees using a protractor		
Critical Background Knowledge from Previous Grade Levels		
• Understand that shapes in different categories may share attributes, and that	at the shared attributes can define a larger category. Recognize rhombuses,	
rectangles, and squares as examples of quadrilaterals, and draw examples of	f quadrilaterals that do not belong to any of these subcategories. (3.G.1)	
• Recognize and draw shapes having specified attributes, such as a given number of the second	ber of sides of angles. Identify and describe quadrilaterals, squares, rectangle	es,
and trapezoids (2.G.1)		
• Identify and distinguish between defining attributes versus non-defining attributes; build and draw shapes that possess defining attributes (1.G.1)		
• Students work with trapezoids, squares, rectangles, triangles, circles, and hexagons in first and second grade. The term quadrilateral is introduced in second		
grade. Rhombuses and parallelograms are introduced in third grade.		
Academic Vocabulary		
classify, right triangle, parallel line, perpendicular line, acute angle, obtuse angle	le, right angle, two-dimensional figure	
,, o o ., p		

Suggested Models	Suggested Strategies
A dt least one set of parallel sides A least one right angle B	 Use graphic organizers such as Venn diagrams, t-charts, etc. Play "Guess My Rule". Select a rule (for example quadrilaterals) start to sort a given set of shapes. Slowly add shapes to the sort. After each shape is added students guess the rule. Sort for examples and non-examples of a given attribute
Closed shape Closed shape 4 sides Opposite sides parallel Perpendicular line segments Opposite sides congruent All sides congruent Right angle(s) Acute angle(s) Obtuse angle(s)	
Image Sources: <u>http://www.dpi.state.nc.us/docs/curriculum/mathematics/scc</u> standards/4/G/A/2/tasks/1275	is/4.pdf; https://www.illustrativemathematics.org/content-

Core Guide Grade 4 Geometry Draw and identify lines and angles, as well as classify shapes by properties of their lines and angles (Standards 4.G.1–3). Standard 4.G.3 Recognize a line of symmetry for a two-dimensional figure as a line across the figure such that the figure can be folded along the line into matching parts. Identify line-symmetric figures and draw lines of symmetry. Concepts and Skills to Master • Recognize the meaning of a line of symmetry as a line that separates two matching parts in a figure • Draw lines of symmetry within a figure • Identify whether or not a figure has a line of symmetry Teacher Note: Fourth grade work is limited to line symmetry. Rotational symmetry, also referred to as point symmetry, is introduced in eighth grade. Related Standards: Current Grade Level Related Standards: Future Grade Levels There are no directly related standards in this grade level, although **8.G.2** Understand congruence by a sequence of rotations, reflection, and recognizing symmetry may related to drawing and classifying shapes (4.G.1. translations 4.G.2) Critical Background Knowledge from Previous Grade Levels • Partition shapes into halves (2.G.3, 1.G.3) • Compose two-dimensional shapes (1.G.2) Academic Vocabulary symmetry, matching parts, line, line of symmetry, symmetrical Suggested Models Suggested Strategies • Use tracing paper to trace a shape and fold along the line of symmetry to recognize the matching parts • Sort shapes into "shapes with a line of symmetry" and "shapes those without a line a symmetry" • Use a geometry mirror to explore whether or not a shape has a line of symmetry • Use geoboards or dot grids to explore shapes and identify whether or not a line of symmetry exists • Find all of the lines of symmetry in a given shape